

## *MODEL almost ANY DATA!*

### SySc 551/651: **DISCRETE MULTIVARIATE MODELING**

In this course, information theory is used as a framework for modeling and data mining: for analyzing static or dynamic relations among discrete\* variables, for detecting complex interaction effects, and for discovering nonlinearities in continuous variables made discrete by binning.

In the systems literature, these information-theoretic and related set-theoretic methods, used together with graph theory techniques, are called “Reconstructability Analysis” (RA). RA overlaps with and extends log-linear modeling in the social sciences, Bayesian networks and graphical models in machine learning, decomposition techniques in multi-valued logic design, Fourier methods for compression, and other modeling approaches. It can be used for confirmatory and exploratory statistical modeling as well as for non-statistical applications.

Because of their applicability to both qualitative and quantitative variables, RA methods are very general. They are usable in the natural sciences, social sciences, engineering, business, and other professional fields. The ideas of RA define “structure,” “complexity,” “holism,” and other basic notions, and are foundational for systems science. For course-related research and publications, see items listed in the Discrete Multivariate Modeling category in my Selected Works website, [https://works.bepress.com/martin\\_zwick/](https://works.bepress.com/martin_zwick/).

This is the theory course that goes with the project course, SySc 431/531 **Data Mining with Information Theory**, next offered in Winter 2023. It is also the theory course for the **Occam software**, recently been made open source; see <https://www.occam-ra.io/>

\*Discrete variables are typically nominal (categorical, symbolic), but may be ordinal or integer.

Prerequisites: Background in probability/statistics.

Texts (at the PSU bookstore):

1. Krippendorff, Klaus (K). *Information Theory: Structural Models for Qualitative Data*. Series: Quantitative Applications in the Social Sciences, Paper # 62, Sage Publications, Beverly Hills, California, 1986. (ISBN 0-8039-2132-2, paperback) *Main* text for course.
2. Knoke, David and Burke, Peter J. (K & B). *Log-Linear Models*. Series: Quantitative Applications in the Social Sciences, paper # 20. Sage Publications, Beverly Hills, California, 1980. (ISBN 0-8039-1492-X, paperback) *Secondary* text for course.

Grades will be based on midterm and final exams and a micro-project.\*

\*If any aspect of this course presents a barrier to your learning, please notify me.

Outline ([ ] = optional or skim)

Jan 8	Course overview <i>Zwick (Overview) [Wholes &amp; Parts] [Introduction to RA]</i>
Jan 10	<b>I Basic concepts</b> (information-theoretic): static/dynamic multivariate relations in categorical data; uncertainty, transmission; <i>K: 1-32</i>
Jan 15	<i>University holiday (no class)</i>
Jan 17, 22	<b>I Basic concepts, continued</b>
Jan 24	<b>II Structures</b> (graph theoretic); degrees of freedom <i>K: 32-43, 47-53 [70-81]; K&amp;B: 36-37</i>
Jan 29	<b>I Basic concepts: exercises</b>
Jan 31	<b>II Structures (continued)</b>
Feb 5	<b>II Structures: <u>exercises</u></b>
Feb 7	<b>III Information-theoretic reconstruction</b> (Putting I & II together) Generalized transmission, information distance; uncertainty maximization; iterative proportional fitting; statistical issues <i>K: 43-62, 66-67, 70-88; K&amp;B: 30-34, 38-42 [Zwick (CU, RAE)]</i>
Feb 12	<b>MIDTERM EXAM</b> on TOPICS I & II only
Feb 14	<b>III Information-theoretic reconstruction</b> (continued)
Feb 19	Over midterm exam
Feb 21	<b>III Information-theoretic reconstruction</b> (continued)
Feb 26	<b>III Information-theoretic reconstruction: <u>exercises</u></b>
Feb 28	<b>IV OCCAM software</b> <i>Willett &amp; Zwick; Fusion, Willett &amp; Zwick; Kramer et al</i>
Mar 4	<b>IV OCCAM software: <u>exercises</u></b>
Mar 6	<b>V Supplementary topics:</b> Binning <i>Zwick, Shu, &amp; Koch,</i> Set-theoretic RA <i>Zwick (CU_4), Zwick &amp; Shu; Zwick (O_II.3)</i> State-based RA <i>Johnson &amp; Zwick, Zwick &amp; Johnson, Zwick (O_II.2)</i>
Mar 11	<b>V Supplementary topics (continued) &amp; <u>exercises</u> (on Mar 6 topics)</b> Log-linear modeling <i>K&amp;B: 5-29, 42-63</i> Reconstruction vs. identification, masks, k-systems
Mar 13	<b>General review; MICRO-PROJECTS DUE</b>
Mar 18	<b>FINAL EXAM:</b> will cover material from <u>entire</u> course, <u>except</u> V topics discussed on Mar 11.

To be distributed in class or available on web/Canvas:

Chi-square table, Midterm and final exams: 2018, 2019, 2021

For Jan 8: Zwick, M. "Reconstructability Analysis Overview for DMM Class" In Canvas.

Associated Papers*For Jan 8*

Zwick, M. "Overview of Reconstructability Analysis (O)." *Kybernetes*, 33 (5-6), 2004, pp. 877-905. [https://works.bepress.com/martin\\_zwick/57/](https://works.bepress.com/martin_zwick/57/)

Zwick, M. "Wholes and Parts in General Systems Methodology." *The Character Concept in Evolutionary Biology*, Gunter Wagner, ed., Academic Press. pp. 237-256, 2001.

[https://works.bepress.com/martin\\_zwick/52/](https://works.bepress.com/martin_zwick/52/)

*For Feb 5*

Zwick, M. "Control Uniqueness in Reconstructability Analysis (CU: not 4)." *Int. J. General Systems*, vol. 24 (1-2), 1996, pp.151-162. [https://works.bepress.com/martin\\_zwick/61/](https://works.bepress.com/martin_zwick/61/)

Zwick, M. "Reconstructability Analysis of Epistasis (RAE)." *Annals Human Genetics* 75(1): 157-171. [https://works.bepress.com/martin\\_zwick/3/](https://works.bepress.com/martin_zwick/3/)

*For Mar 4*

Willett, K. & Zwick, M. "A Software Architecture for Reconstructability Analysis." *Kybernetes*, 33 (5-6), 2004, pp. 997-1008. [https://works.bepress.com/martin\\_zwick/55/](https://works.bepress.com/martin_zwick/55/)

Zwick, M (2016). "OCCAM: A Reconstructability Analysis Program." OCCAM Manual at [https://works.bepress.com/martin\\_zwick/164/](https://works.bepress.com/martin_zwick/164/)

Kramer, P., Westaway, S., Zwick, M., and Shervais, S. (2012) "Reconstructability Analysis of Genetic Loci Associated with Alzheimer Disease." *IEEE 6th International Conference on Soft Computing & Intelligent Systems & 13th International Symposium on Advanced Intelligent Systems*, SCIS-ISIS2012, Kobe, Japan, Nov. 20-24, 2012.

[https://works.bepress.com/martin\\_zwick/92/](https://works.bepress.com/martin_zwick/92/)

*For Mar 11*

Zwick, M., Shu, H., & Koch, R. "Information-Theoretic Mask Analysis of Rainfall Time Series Data." *Advances in Systems Science and Applications* (1995), Special issue 1, pp. 154-159.

[https://works.bepress.com/martin\\_zwick/148/](https://works.bepress.com/martin_zwick/148/)

Zwick, M. & Shu, H. "Set-Theoretic Reconstructability of Elementary Cellular Automata." *Advances in Systems Science and Applications* (1995), Special issue 1, pp. 31-36.

[https://works.bepress.com/martin\\_zwick/79/](https://works.bepress.com/martin_zwick/79/)

Johnson, M.S. and Zwick, M. "State-Based Reconstructability Modeling for Decision Analysis." *Proceedings of World Congress of the Systems Sciences & 44th Annual Meeting of the International Society for the Systems Sciences*, Toronto, July 16-22, 2000.

[https://works.bepress.com/martin\\_zwick/74/](https://works.bepress.com/martin_zwick/74/)

Zwick, M. & Johnson, M. "State-Based Reconstructability Analysis." *Kybernetes*, 33 (5-6), 2004, pp. 1041-1052; *Proceedings of 12<sup>th</sup> International World Organization of Systems and Cybernetics and 4<sup>th</sup> International Institute for General Systems Studies Workshop*, Pittsburgh, March 24-26.

[https://works.bepress.com/martin\\_zwick/47/](https://works.bepress.com/martin_zwick/47/)