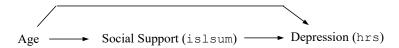
Testing Mediation with Regression Analysis Examples

1

SPSS

Below I use an SPSS macro developed Andrew Hayes (see Hayes & Rockwood, 2017) to test an indirect effect using the Yale social support data. The "Process" macro can be downloaded from: http://www.processmacro.org/download.html. In this example, age (age) is the predictor, social support (islsum) is the mediator, and depression (hrs) is the final outcome. Here is a picture of the model:



After downloading the macro, save it in a known location that you can specify the exact path for. Create a new syntax file and either open your data set or add a get file='your data set location and file name here' command to the beginning of the syntax file to specify the location of your data file. Then add the following commands (this was tested with Process version 4.3 syntax), replacing your variable names for my variable names for X (initial predictor), Y (final outcome), and Y (mediator) to the syntax file:

```
cd "c:\jason\temp".
insert file='C:\Jason\SPSSWIN\macros\process.sps'.
execute.
process y = hrs
    / x = age
    / m = islsum
    /total=1
    /boot=10000
    /seed=10000
    /model=4
    /stand=1.
execute.
```

Make sure that the <code>insert file</code> command points to the exact location of the process macro where you saved it. Then, highlight the entire syntax in the syntax window, and run. <code>/effsize=1</code> can also be used to obtain standardized coefficients.

Output

The first section of the output (marked by lines of asterisks) gives each of the direct regression coefficients depicted in the diagram above and will be the same as those you would obtain with the usual regression command in SPSS. The bootstrap tests of the indirect effect are found in the final section under the heading "TOTAL, DIRECT, AND INDIRECT EFFECTS OF X ON Y" and then under the subheading "Indirect effect (s) of X on Y:", where Effect gives the average estimate for indirect effect from the bootstrap samples, BootSE gives the standard error estimate, and BootLLCI and BootULCI are 95% confidence limits. If the 95% confidence limits include zero, the indirect effect test is not significant.²

¹ Mac locations have no drive letter and forward slashes, '/Users/your subfolders'

² Note that these limits are "percentile" limits which do not involve a bias correction ("accelerated confidence limits"), as the bias-corrected limits may have slightly elevated Type I error rates (Fritz, Taylor, & MacKinnon, 2012; Hayes & Scharkow, 2013).

1 3y 322/022 WI	unipie regressi	on and Mariva	nate Quantitativ	e Methods, W	THE 2024	
Sample Size: 301						
Custom Seed: 10	0000					
*************** OUTCOME VAR:		*****	******	*****	*****	*****
Model Summa: R .0277	R-sq	MSE 5.2515		df1 1.0000	df2 299.0000	p .6316
Model						
constant age	coeff 12.6950 0046	se .6110 .0096	t 20.7788 4800	p .0000 .6316	LLCI 11.4927 0236	ULCI 13.8973 .0143
	d coefficien eff 277	ts				
3			*****			
OUTCOME VAR				^^^^		
Model Summa: R	R-sq	MSE		df1	df2	р
.3329	.1109	30.5137	18.5762	2.0000	298.0000	.0000
Model	coeff	se	t	q	LLCI	ULCI
constant age	20.7583	2.3023	9.0162 -2.5304	.0000	16.2274 1045	25.2892 0131
islsum	7825	.1394	-5.6133	.0000	-1.0569	5082
	d coefficien	ts				
_	1383 3067					
************* OUTCOME VAR		*** TOTAL 1	EFFECT MODEL	* * * * * * * * * *	*****	****
Model Summa:	ry					
.1298	R-sq .0168	MSE 33.6273	F 5.1205	df1 1.0000	df2 299.0000	.0244
Model	coeff	se	ŧ	n	LLCI	III.CT
constant age	10.8243	1.5460	7.0014 -2.2629	.0000	7.7819 1032	13.8668
Standardized coe age12		ts				
*****	*** TOTAL, D	IRECT, AND	INDIRECT EF	FECTS OF X	ON Y ****	****
Effect		t	p .0244			c_cs 1298
	ct of X on Y		. 72.11	. 1002		11230
Effect	se	t	.0119			c'_cs 1383

BootSE BootLLCI BootULCI

-.0134

.0196

.0081

Indirect effect(s) of X on Y:

Effect

.0036

islsum

```
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Completely standardized indirect effect(s) of X on Y:
         Effect BootSE BootLLCI BootULCI
                     .0188
                             -.0307
           .0085
                                           .0461
islsum
******************* ANALYSIS NOTES AND ERRORS *****************
Level of confidence for all confidence intervals in output:
  95.0000
Number of bootstrap samples for percentile bootstrap confidence intervals:
  10000
----- END MATRIX -----
#clear active frame from previous analyses
rm(d)
```

library(haven)
d = read_sav("c:/jason/spsswin/da2/yale.sav")

```
#listwise deletion necessary to make sample sizes for the two regressions match
> library(dplyr)
> d <-filter(d,age != 'NA' & islsum!='NA' & hrs!='NA')

library(mediation)
#specify two separate models, one predicting the mediator, m, and one predicting the outcome, y
# covariates can be included in either model
mmodel <-lm(islsum ~ age, data = d)
ymodel <- lm(hrs ~ islsum + age, data = d)
summary(mmodel)
summary(ymodel)
rm(medtest)</pre>
```

#request the boostrap indirect test, default is 1000 samples (usually ok),
#"perc" requests standard percentiles or use "bca" is for bias-corrected version (not recommended)
medtest <- mediate(mmodel, ymodel, treat = "age", mediator = "islsum", boot.ci.type = "perc", data = d)</pre>

The separate regressions are printed but omitted here for brevity. The output reports the "Estimate", which is the average indirect coefficient of the bootstrap samples, the 95% confidence intervals, and the p-value for significance test. The indirect coefficient is reported for the row labeled "ACME", which stands for average causal mediation effects, and the direct effect of X predicting Y controlling for the mediator is labeled "ADE",

causal mediation effects, and the direct effect of *X* predicting *Y* controlling for the mediator is labeled "ADE", which stands for average direct effect. The total effect is the two of these effects added together. The proportion mediated attempts to capture the portion of the total effect that is due to the mediation effect (details of the computations of this quantity vary).

or the computations of the quantity

Quasi-Bayesian Confidence Intervals

```
Estimate 95% CI Lower 95% CI Upper p-value
               0.00376
-0.05894
                                       0.02
-0.01
ACMF
                            -0.01067
                                                      0.642
                            -0.10446
                                                      0.010
ADF
Total Effect
                             -0.10348
               -0.05518
                                             -0.01
                                                      0.024
Prop. Mediated -0.05913
                             -0.87580
                                                      0.662
```

Sample Size Used: 301

Causal Mediation Analysis

Simulations: 1000

summary(medtest)

Alternatively, the RMediation package (see Tofighi & MacKinnon, 2011) to estimate the confidence limits with the Monte Carlo method, which performs similarly to the percentile bootstrap method in most cases but may have slightly better power for indirect effects across multiple direct paths when effect sizes are more modest (Tofighi & MacKinnon, 2015). Values from prior regressions need to be input into the medci function, where mu.x and mu.y refer to the a and b paths and se.x and se.y refer to their respective standard errors.

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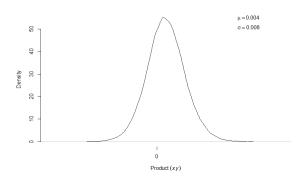
> #plug in results for mu.x (a path) and mu.y (b path) and their SEs from the mediation regressions
> medci(mu.x=-.0046,mu.y=-.7825,se.x=.0096,se.y=.1394,rho=0,alpha=.05,type="MC") \$`97.5% CI` 2.5% 97.5% -0.01129172 0.01922726

\$Estimate [1] 0.003624395

library(RMediation)

\$SE [1] 0.0076663

\$`MC Error [1] 0.000000076663



References

- Fritz, M. S., Taylor, A. B., & MacKinnon, D. P. (2012). Explanation of two anomalous results in statistical mediation analysis. Multivariate behavioral research, 47(1), 61-87.
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- Hayes, A. F., & Scharkow, M. (2013). The relative trustworthiness of inferential tests of the indirect effect in statistical mediation analysis: Does method really matter?. Psychological science, 24(10), 1918-1927.
- Shrout, P. E., & Bolger, N. (2002). Mediation in experimental and nonexperimental studies: new procedures and recommendations. Psychological methods, 7(4), 422.
- Tingley, D., Yamamoto, T., Hirose, K., Keele, L., & Imai, K. mediation: R Package for Causal Mediation Analysis. https://cran.rproject.org/web/packages/mediation/vignettes/mediation.pdf.
- Tofighi, D., & MacKinnon, D. P. (2011). RMediation: An R package for mediation analysis confidence intervals. Behavior Research Methods, 43, 692-700.
- Tofighi, D., & MacKinnon, D. P. (2015). Monte Carlo Confidence Intervals for Complex Functions of Indirect Effects. Structural Equation Modeling: A Multidisciplinary Journal, 1-12

Example Mediation Write-up

Sadly, my example above was not significant \odot , so I did another example that would be \odot for use in an example write-up. The output from the macro is included again here to see where the results came from. The example was an investigation of the hypothesis that therapy affects satisfaction by affecting attributional positivity.

Steps are the same as above, and here are the modified command lines.

```
cd "c:\jason\temp".
insert file='C:\Jason\SPSSWIN\macros\process.sps'.
execute.
process y = satis
 / x = therapy
 / m = attrib
 /total=1
 /boot=10000
 /seed=10000
 /model=4
 /stand=1.
execute.
********************
OUTCOME VARIABLE:
attrib
Model Summary
                            MSE F
.6676 7.4940
                 R-sq
.2111
                                                 df1
                                                            df2
         R
                                               1.0000
                                                          28.0000
      .4595
                .2111
Model
             coeff
                           se
                                                  р
                                       t
                                                                      ULCI
                                                           TJT,CT
                                                .1166
constant
             -.3536
                         .2184
                                 -1.6191
                                                         -.8009
                                                                       .0938
                         .2990 2.7375
             .8186
                                                .0106
                                                           .2060
                                                                     1.4311
therapy
Standardized coefficients
             coeff
             .9056
therapy
****************
OUTCOME VARIABLE:
satis
Model Summarv
      R R-sq MSE F df1 df2 .5566 .3098 .6112 6.0605 2.0000 27.0000
                                                                          .0067
Model

        se
        t
        p
        LLCI

        .2185
        -.8437
        .4063
        -.6327

        .3221
        1.3455
        .1897
        -.2275

        .1808
        2.2337
        .0340
        .0329

             coeff
             -.1843
                                                                      .2640
constant.
           .4334
therapy
                                                                    1.0944
             .4039
attrib
Standardized coefficients
       coeff
             .4773
therapy
             .4021
attrib
************************* TOTAL EFFECT MODEL *********************
OUTCOME VARIABLE:
 satis
Model Summary
                                      F
         R
                 R-sq MSE F
.1823 .6982 6.2421
                                                    df1
                                                                df2
                                                          28.0000
                                                1.0000
                                                                     .0186
      .4270
```

coeff se t p LLCI ULCI constant 3271 .2233 -1.4649 .1541 7846 .1303 therapy .7640 .3058 2.4984 .0186 .1376 1.3904 Standardized coefficients coeff Coeff therapy .8414 ***********************************	Model	6.6			-					
<pre>therapy</pre>	constant	COEII - 3271	se 2233	-1 4649						
Standardized coefficients coeff therapy .8414 **********************************										
coeff therapy .8414 **********************************	chcrapy	. 7010	.5050	2.1501	.0100	.1370	1.0001			
therapy	Standardized coefficients									
**************************************		coeff								
Total effect of X on Y Effect se t p LLCI ULCI c_ps .7640 .3058 2.4984 .0186 .1376 1.3904 .8414 Direct effect of X on Y Effect se t p LLCI ULCI c'ps .4334 .3221 1.3455 .18972275 1.0944 .4773 Indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI attrib .3306 .1702 .0377 .7004 Partially standardized indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI	therapy	.8414								
Total effect of X on Y Effect se t p LLCI ULCI c_ps .7640 .3058 2.4984 .0186 .1376 1.3904 .8414 Direct effect of X on Y Effect se t p LLCI ULCI c'ps .4334 .3221 1.3455 .18972275 1.0944 .4773 Indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI attrib .3306 .1702 .0377 .7004 Partially standardized indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI										
Effect se t p LLCI ULCI c ps .7640 .3058 2.4984 .0186 .1376 1.3904 .8414 Direct effect of X on Y	*****	** TOTAL, DI	RECT, AND	INDIRECT EF	FECTS OF X	ON Y ****	*****			
Effect se t p LLCI ULCI c ps .7640 .3058 2.4984 .0186 .1376 1.3904 .8414 Direct effect of X on Y	motal offort	of V on V								
.7640 .3058 2.4984 .0186 .1376 1.3904 .8414 Direct effect of X on Y Effect se t p LLCI ULCI c'ps .4334 .3221 1.3455 .18972275 1.0944 .4773 Indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI attrib .3306 .1702 .0377 .7004 Partially standardized indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI			+	n	T.T.C.T	III.CT	c ns			
Direct effect of X on Y Effect se t p LLCI ULCI c'_ps .4334 .3221 1.3455 .18972275 1.0944 .4773 Indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI attrib .3306 .1702 .0377 .7004 Partially standardized indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI										
Effect se t p LLCI ULCI c'ps .4334 .3221 1.3455 .18972275 1.0944 .4773 Indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI attrib .3306 .1702 .0377 .7004 Partially standardized indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI										
.4334 .3221 1.3455 .18972275 1.0944 .4773 Indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI attrib .3306 .1702 .0377 .7004 Partially standardized indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI	Direct effec	t of X on Y								
Indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI attrib .3306 .1702 .0377 .7004 Partially standardized indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI										
Effect BootSE BootLLCI BootULCI attrib .3306 .1702 .0377 .7004 Partially standardized indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI	.4334	.3221	1.3455	.1897	2275	1.0944	.4773			
Effect BootSE BootLLCI BootULCI attrib .3306 .1702 .0377 .7004 Partially standardized indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI										
attrib .3306 .1702 .0377 .7004 Partially standardized indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI		. ,		attict Das	LIII OT					
Partially standardized indirect effect(s) of X on Y: Effect BootSE BootLLCI BootULCI										
Effect BootSE BootLLCI BootULCI	acciib	.5500	1702	.0377	. 7004					
Effect BootSE BootLLCI BootULCI	Partially standardized indirect effect(s) of X on Y:									
attrib .3641 .1856 .0455 .7677	-									
***************************************	attrib	.3641	1856	.0455	.7677					

Write-up

Regression analysis was used to investigate the hypothesis that social support mediates the effect of age on depression. Results indicated that therapy was a significant predictor of attributional positivity, B = .82, SE = .30, 95%CI[.21,1.43], β = .91, p = .01, and that attributional positivity was a significant predictor of satisfaction, B = .404, SE = .181, 95%CI[.03,.77], β = .40, p = .03. Approximately 31% of the variance in satisfaction was accounted for by the predictors (R² = .31). The indirect effect was tested using a percentile bootstrap estimation approach with 10000 samples (Shrout & Bolger, 2002), implemented with the PROCESS macro Version 4.2 beta (Hayes, 2017).³ These results indicated the indirect coefficient was significant, B = .33, SE = .17, 95%CI[.04,.70], partially standardized β = .36.⁴ Receiving therapy was associated with satisfaction scores that were approximately .33 points higher as mediated by attributional positivity. Because therapy was no longer a significant predictor of satisfaction after controlling for the mediator, attributional positivity, B = .43, SE = .32, 95%CI[-.23,1.09], β = .47, p = .19, the results are consistent with full mediation.

Note: I am always cautious about using causal language and so saying something like the results "support the mediational hypothesis" or are "consistent with the mediational hypothesis" is preferrable. This applies to any application, even experimental, but especially when data are cross-sectional and nonexperimental.

³ Hayes, A. F. (2022). *Introduction to mediation, moderation, and conditional process analysis: A regression-based approach, third edition.* Guilford Publications.

⁴ Only the partially standardized coefficient was produced by PROCESS in this example because the predictor was dichotomous. In this case, PROCESS standardizes the outcome variable and mediator but not predictor variable because it is dichotomous. The partially standardized indirect coefficient therefore represents the standard deviation difference in y in the two therapy groups as mediated by attributional positivity.