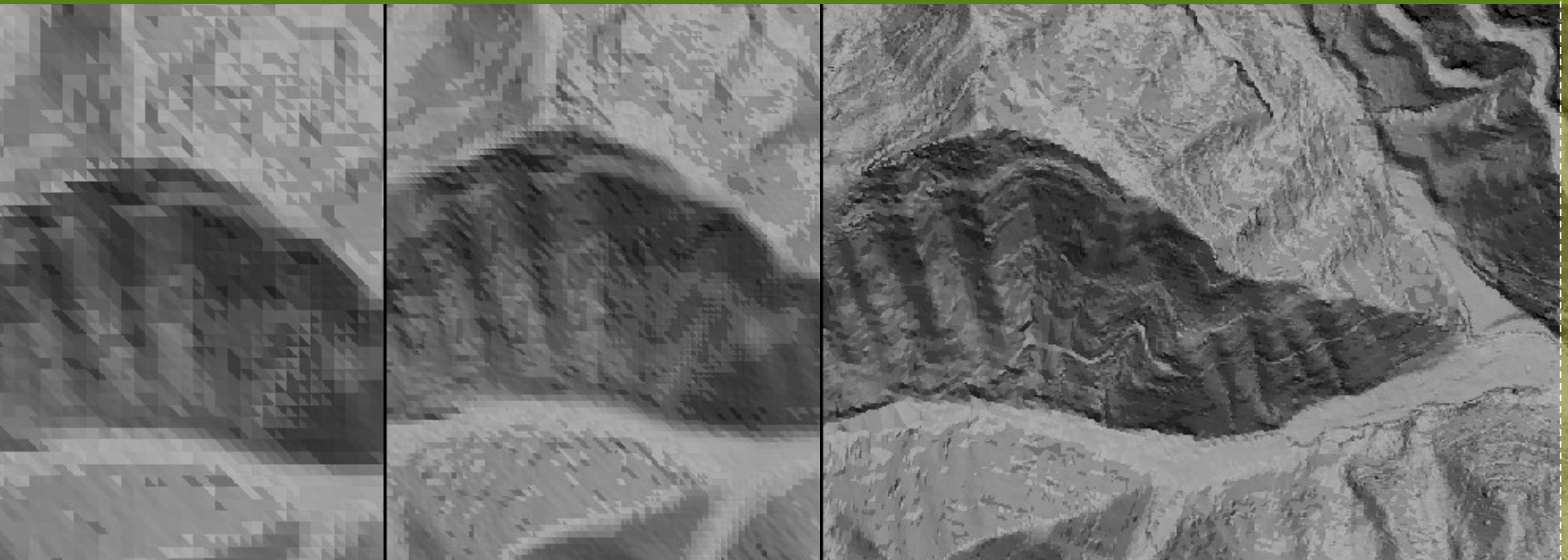


# Course Overview & Digital Terrain Data Models



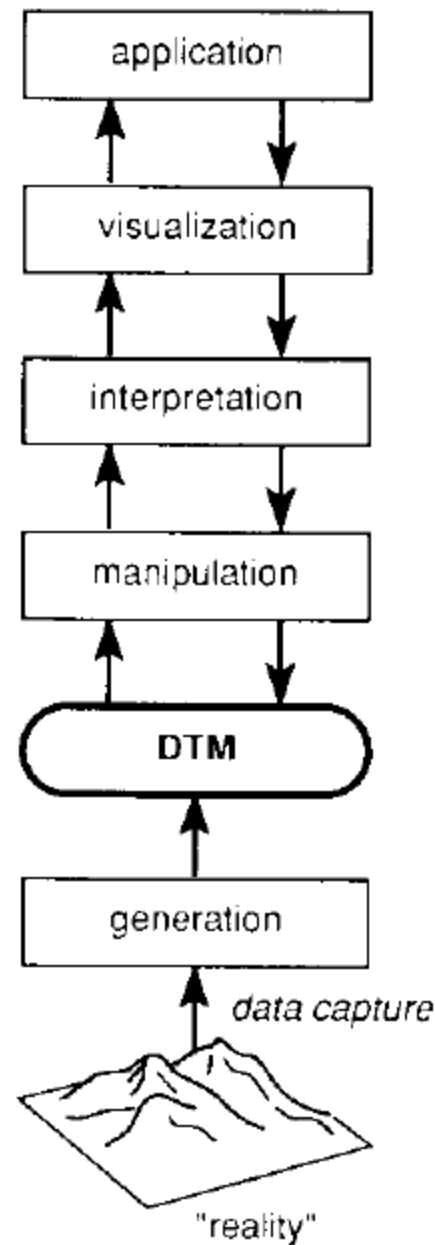


Figure 19.1 The main tasks of a digital terrain modelling system. (Weibel and Heller 1988)

# Digital Terrain

A digital representation of terrain surfaces.

- 2D, 2.5D, or 3D (?)

Representation of terrain surfaces:

- Maps (graphics)
- Physical models
- Mathematical models
- Digital terrain models

# Digital Terrain Models (DTM)

- Trend surfaces (models)
- Digital contour lines
- Elevation points
- DEM
- TIN
- Object with z attribute
- Fractal

# Fractal Terrain (created in Vue)



# Why are DTMs Required?

- Geographic processes
  - Watershed
  - Drainage network
  - Slope, aspect (solar illumination)
  - Viewshed
  - Analyzing volumetric change
  - Orthorectification
  - 3D simulation and visualization
  - ...

# Digital Terrain Surface Modeling

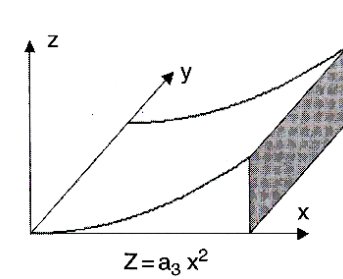
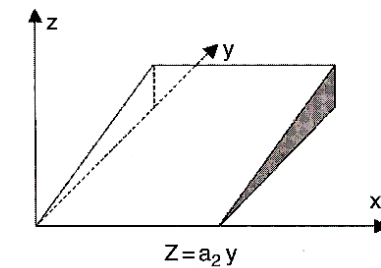
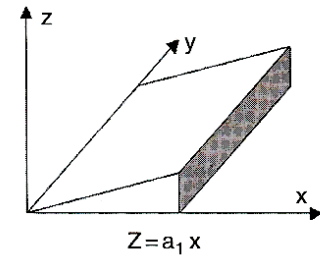
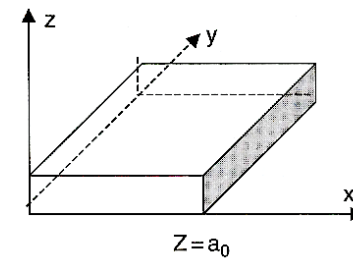
- Data features (points, triangles, grids)
- Surface models
  - Surface interpolation
- Surface reconstruction

# Trend Surface Analysis

Data features: points

Surface models: Polynomial Functions

| Individual Terms   | Order  | Descriptive Terms | No. of Terms |
|--|--------|-------------------|--------------|
| $Z = a_0$  | Zero   | Planar            | 1            |
| $+a_1X + a_2Y$   | First  | Linear            | 2            |
| $+a_3X^2 + a_4Y^2 + a_5XY$   | Second | Quadratic         | 3            |
| $+a_6X^3 + a_7Y^3 + a_8X^2Y + a_9XY^2$   | Third  | Cubic             | 4            |
| $+a_{10}X^4 + a_{11}Y^4 + a_{12}X^3Y + a_{13}X^2Y^2 + a_{14}XY^3$                | Fourth | Quartic           | 5            |
| $+a_{15}X^5 + a_{16}Y^5 + a_{17}X^4Y + a_{18}X^3Y^2 + a_{19}X^2Y^3 + a_{20}XY^4$ | Fifth  | Quintic           | 6            |





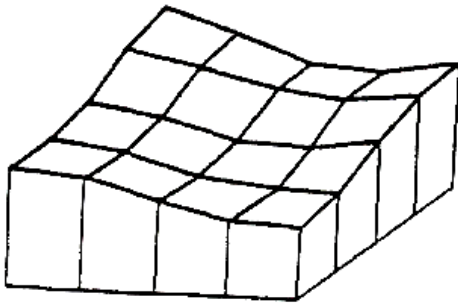
# Minimum Number of Points to Construct a Surface

$$N = \frac{(t+1)(t+2)}{2}$$

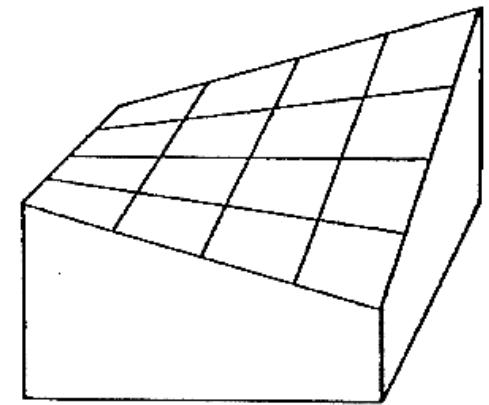
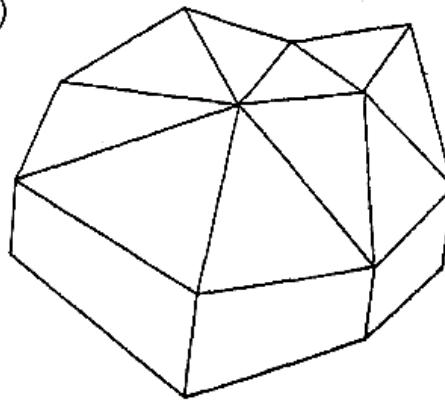
| Order (t) | Type      | Min # Pcts |
|-----------|-----------|------------|
| 0         | Planar    | 1          |
| 1         | Linear    | 3          |
| 2         | Quadratic | 6          |
| 3         | Cubic     | 10         |
| -         | Bi-linear | 4          |

# Bilinear Surface & Bilinear Interpolation

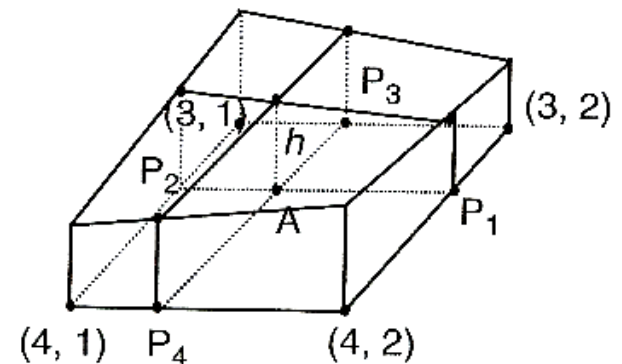
(a)



(b)

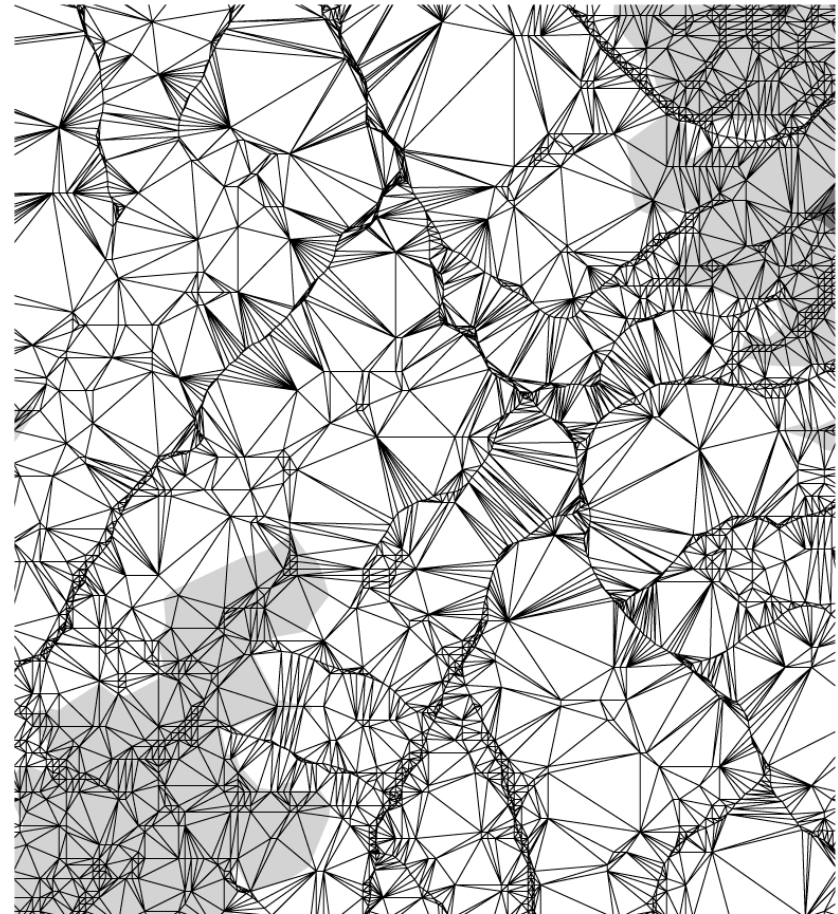


- (a) Surface formed by bilinear surfaces  
(b) Surface formed by triangles



# Triangulated Irregular Network (TIN)

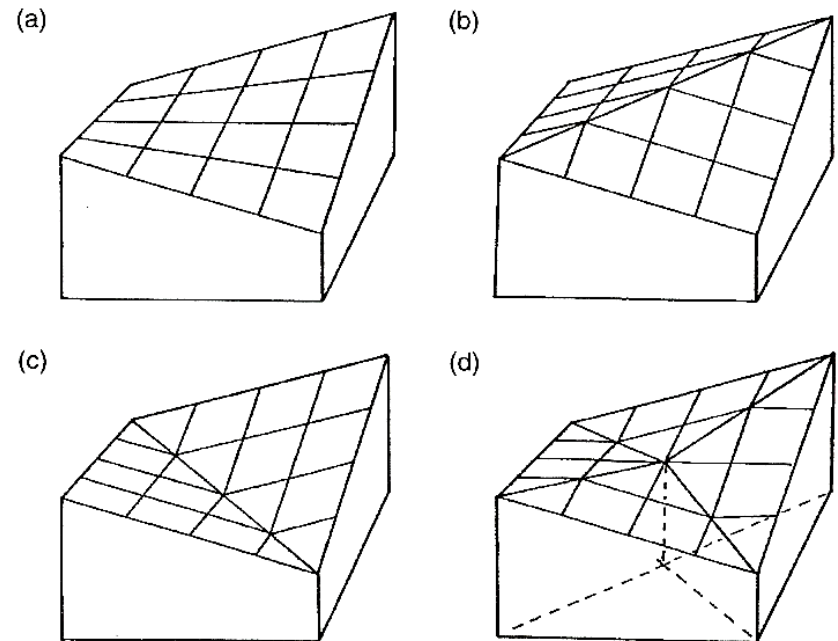
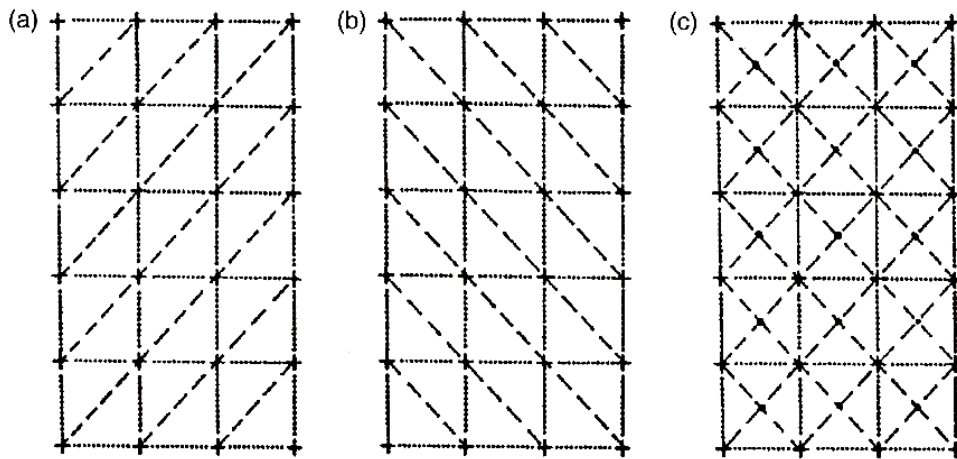
- Node ( $x, y, z$ )
- Edge
- Triangles
- Topology
  - The triangle number
  - The numbers of each adjacent triangle
  - The three nodes defining the triangle
  - The  $x, y$  coordinates of each node
  - The surface  $z$  value of each node
  - The edge type of each triangle edge (hard or soft)

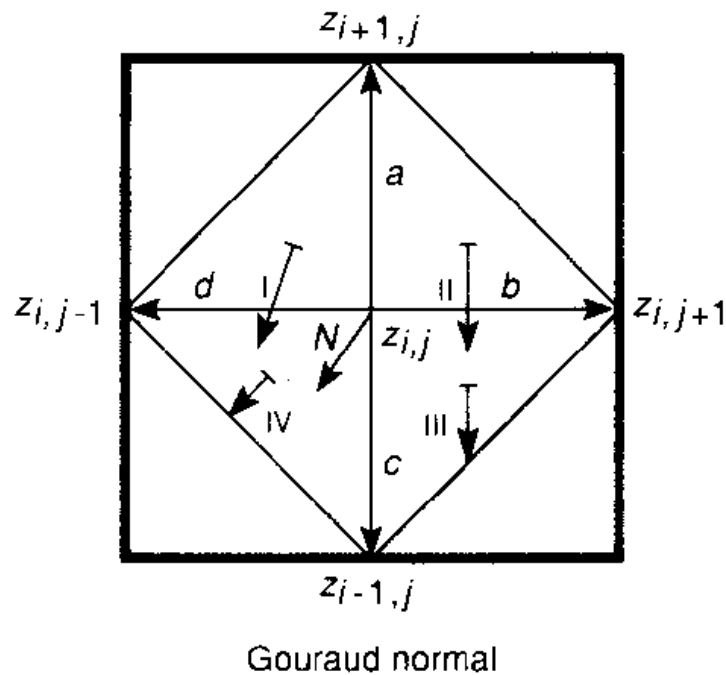
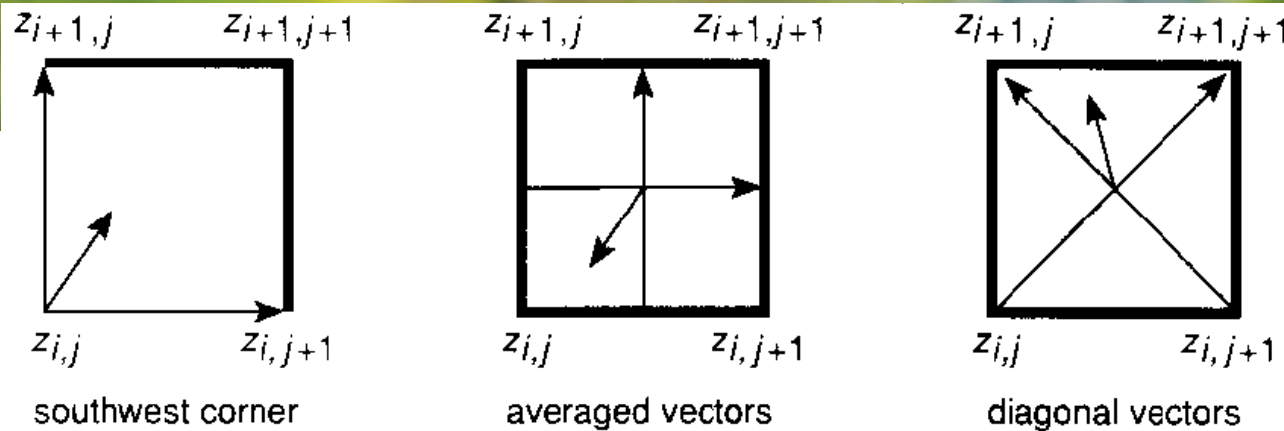


# Hybrid Surface Modeling

Triangular regular network

- Formed from regularly distributed data





$$\begin{aligned} \text{I} &= d \times a \\ \text{II} &= a \times b \\ \text{III} &= b \times c \\ \text{IV} &= c \times d \end{aligned}$$

$$N = (\text{I} + \text{II} + \text{III} + \text{IV}) / 4$$

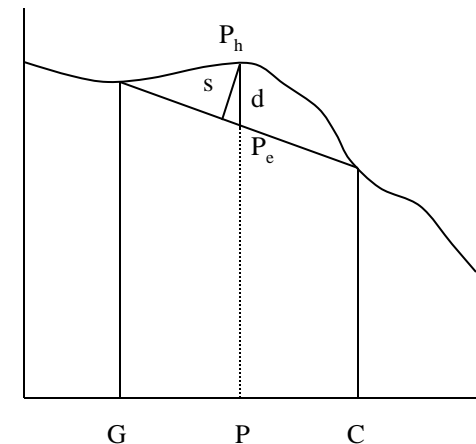
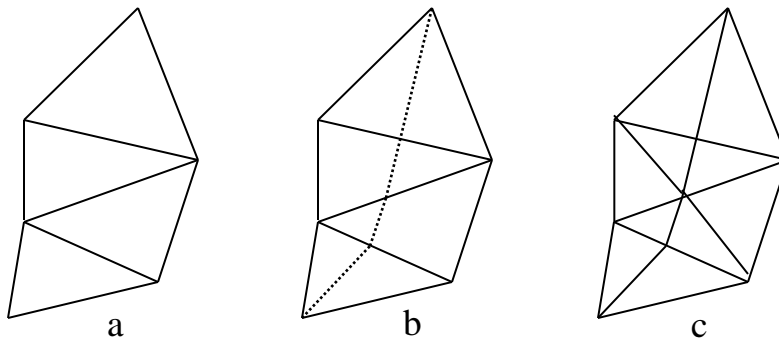
**Fig. 19.11** Several alternatives to obtain averaged surface normals for square patches of either four or nine adjacent grid points.

# Conversions between Surface Models

| <div> <div>To</div> <div>From</div> </div> | Point  | Triangle       | Grid  |
|--|--|----------------|---|
| Point                                      | Spatial interpolation                        | TIN generation | Spatial interpolation, indirect interpolation |
| Triangle                                   | Edge points                                  | -NA-           | Linear / curved surface interpolation         |
| Grid                                       | Nearest neighbor, linear/cubic interpolation | TIN generation | Nearest neighbor, linear/cubic interpolation  |

# Generating TIN

- Selection of significant points from DEM
  - Very Important Points (VIP)
  - Maximum z-tolerance
- Delaunay triangulation
  - Mass points (-> TIN nodes)
  - Breaklines - soft (form), hard (-> TIN edges)





# DEM & DSM

DEM: Digital Elevation Model (ground elevation)

DSM: Digital Surface Model (surface elevation, including trees, buildings, houses, etc)



# Math Review

## Similar triangles

<http://www.mathopenref.com/similartriangles.html>

Known:  $x_0$ ,  $y_0$ ,  $x_1$ ,  $y_1$ , and  $x$

Find:  $y$

Example:

$$x_0, y_0 = 3, 2$$

$$x_1, y_1 = 6, 6$$

$$x = 4$$

$$y = ?$$

