

Remote Sensing Glacier Depth and Correlating Cirque Curvature with Glacial Area

Glacier National Park,
MT

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Introduction

- ▶ Continued research of Mike's Stats project
(correlations of weather and topography)
- ▶ Curvature of cirques
 - with and without ice
 - quantify findings

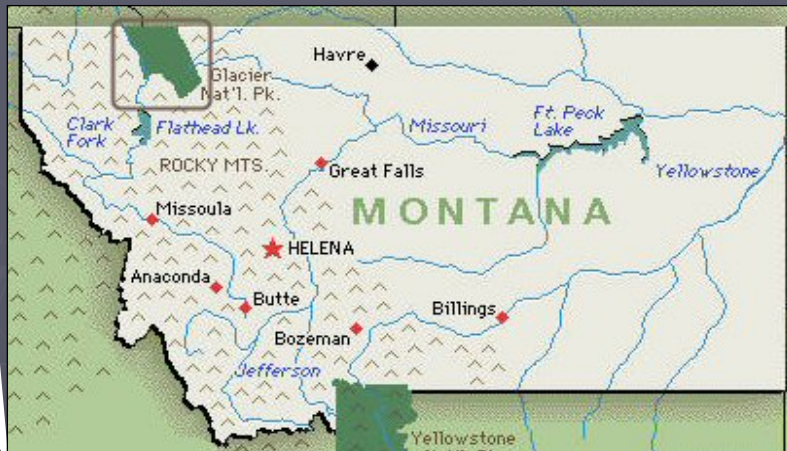


Tools Used

- ▶ ArcGIS
 - 3-D Analyst
 - Spatial Analyst
 - Raster Calculator
 - Conversion
- ▶ ArcScene
- ▶ SPSS
 - Statistical Regression Analysis
- ▶ Excel
 - Graphing

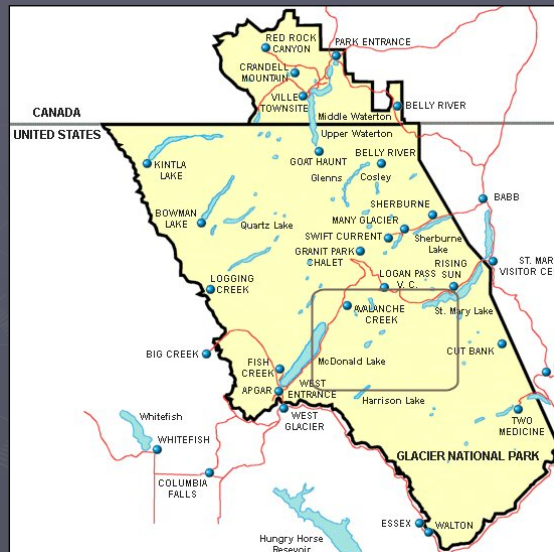


Study Area: Glacier National Park



Source: Greenwich 2000 Ltd.

Study Area: Glacier National Park



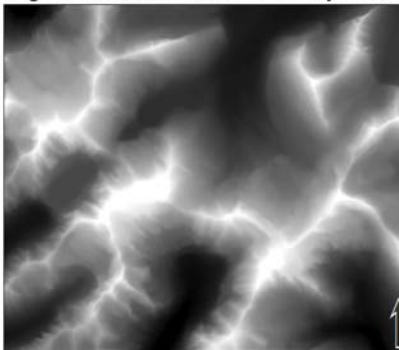
Source: AreaTravelPackets.com

Study Area: Glacier National Park



Source: www.nps.gov/glac

Glacier National Park, Montana
Digital Elevation Model of Study Area



DEM (in meters)



Source: USGS

Glacier National Park, Montana Hillshade Overlay in Study Area

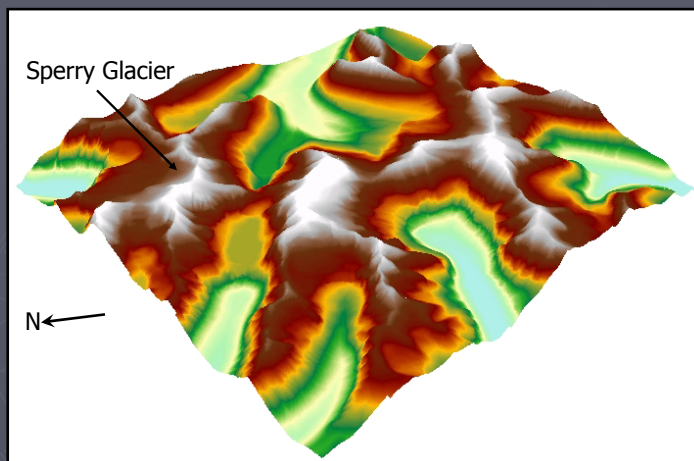


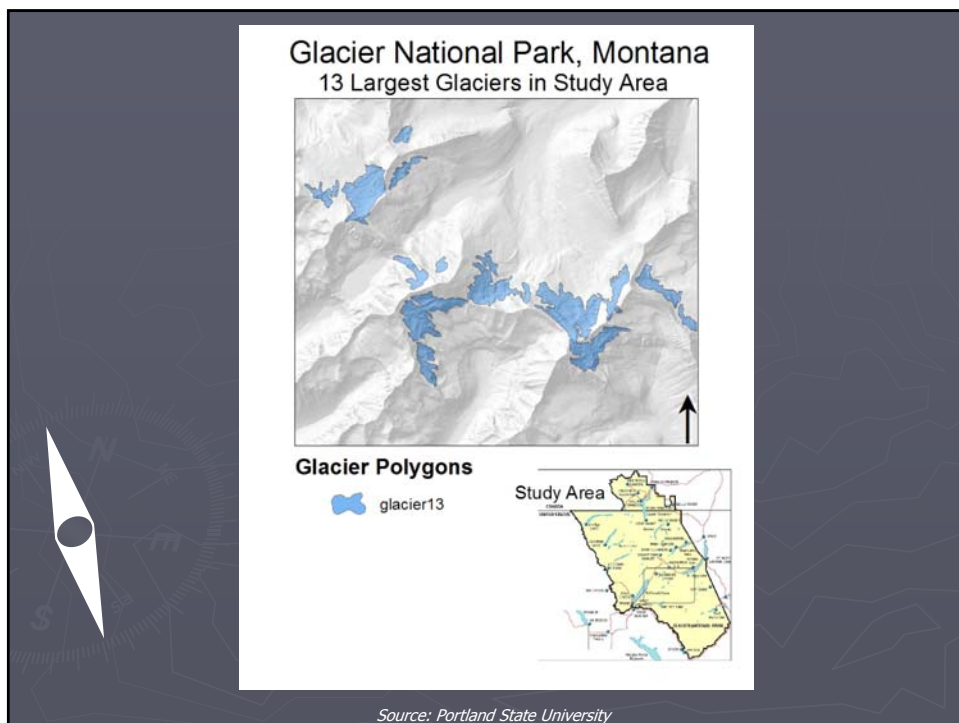
1:74,045

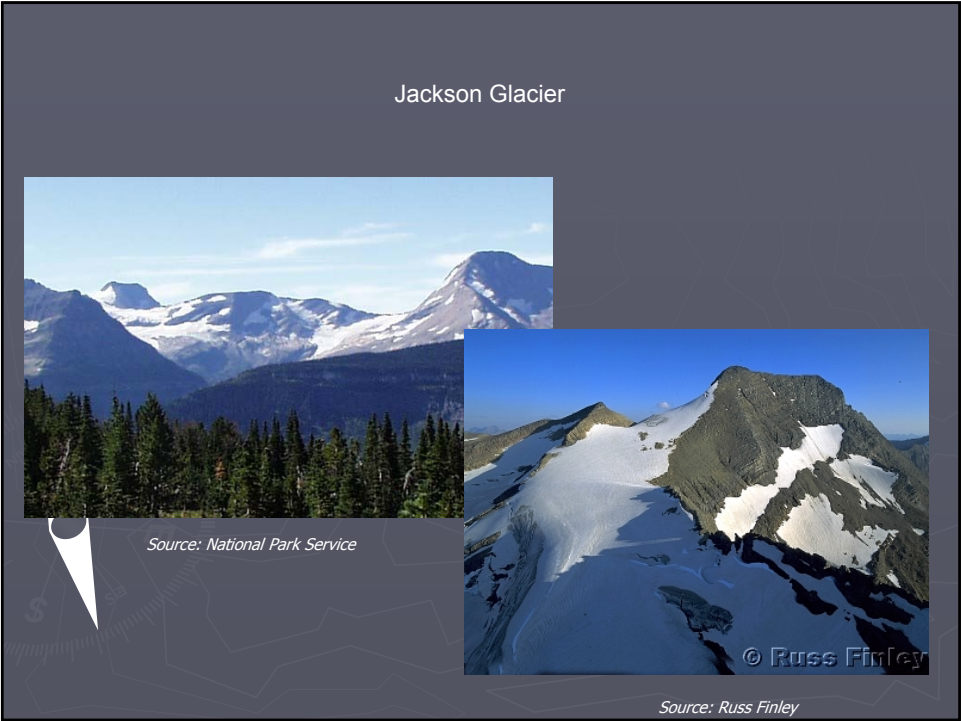
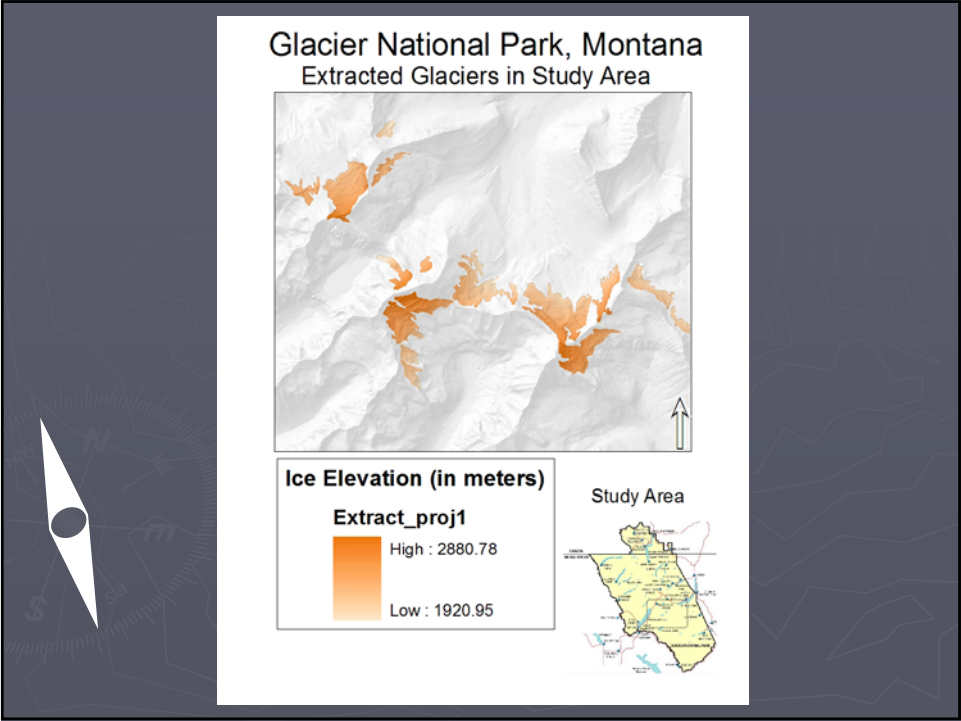
Site Map



ArcScene image of Study Area







Sperry Glacier, at base of Mt. Edwards Glacier National Park



*Morton Elrod photo 1907
Courtesy Glacier NP Archives*



Lisa McKeon photo, 2001 USGS

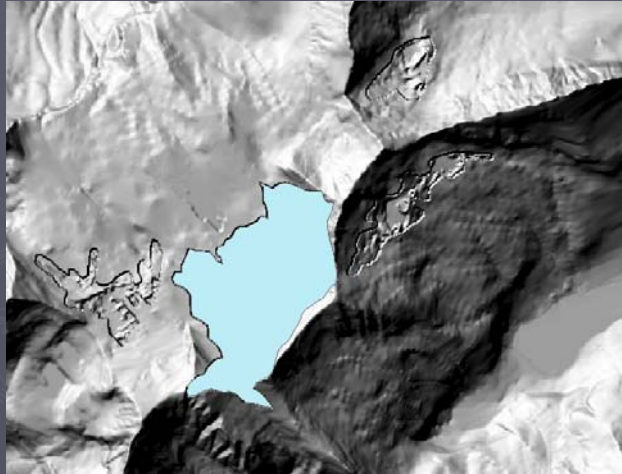
Prior Cirque Research

- ▶ Cirque width, high steep walls, facing northeast determine glacier locations¹
- ▶ Eastward cirque aspect caused by leeward slopes²
- ▶ Morphometric analysis using GIS, C++, and R was useful in delineating landforms³
- ▶ Correlations between cirque morphology and solar radiation and glacier area⁴

¹Graf, 1976; ²Evans, 1977; ³Bonk 2002; ⁴Chueca and Julian, 2004

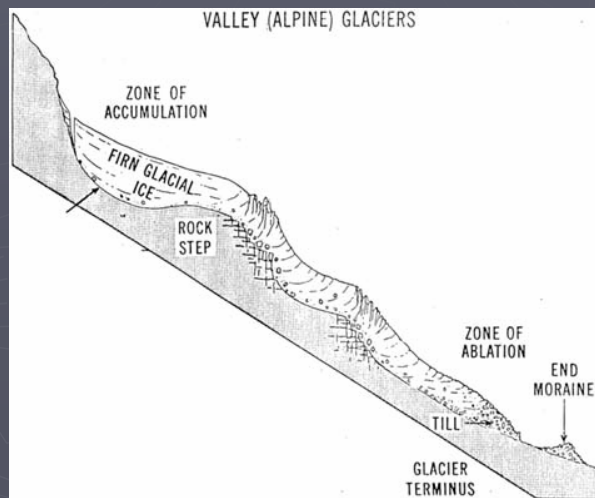
Methods: Remote Sensing of Ice Depth

► Area




Methods: Remote Sensing of Ice Depth

► Surface slope




Methods: Slope-derived Ice Depth


$$T_b / \rho g \sin \alpha = h$$

where $T_b = 1 \text{ bar} = 100,000 \text{ N/m}^2 = \text{kgm/s}^2/\text{m}^2$ *

and $\rho = 890 \text{ kg/m}^3$ *




and $g = 9.8 \text{ m/s}^2$

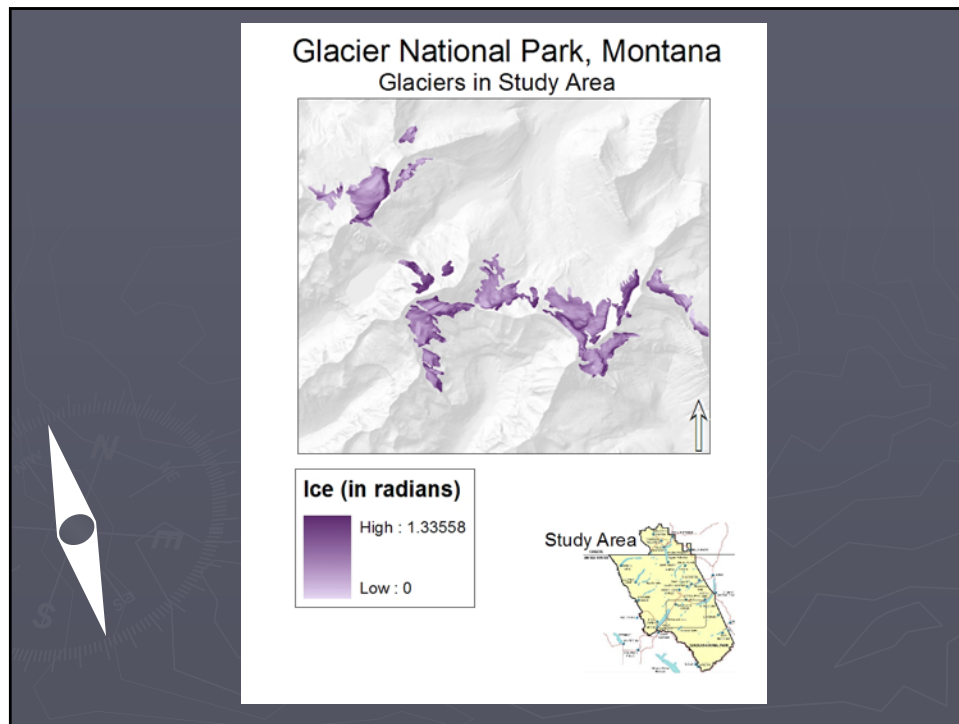

$$11.46526 \text{ m}^3 / \sin \alpha = h$$

* Assumption based on data from Paterson

Source: Paterson 1994

Methods: Ice Depth Calculations

- 
- ▶ Reproject in UTM – bilinear resampling
 - ▶ Slope tool – calculated in degrees
 - ▶ Convert degrees to radians
 - ▶ Use derived ice depth formula using radians value



Raster Calculator

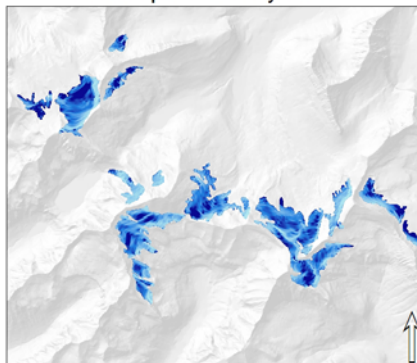
con([glac_rad] < .191088, 19227, [glac_rad])

Depth calculation

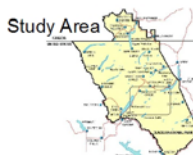
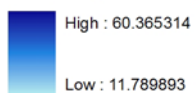
Setting the limit

11.46526 / Sin([Calculation])

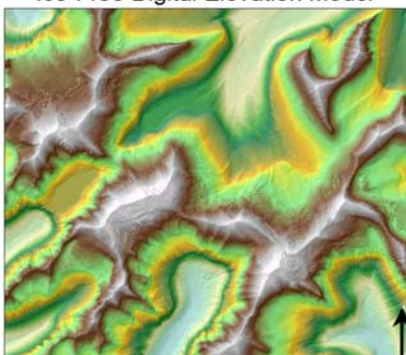
Glacier National Park, Montana Ice Depth in Study Area



Ice Depth (in meters)

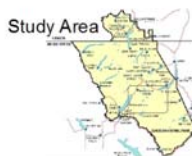


Glacier National Park, Montana Ice-Free Digital Elevation Model



Ice-Free DEM (in meters)

icefreedom



Methods: Depth Calculation Via Volume

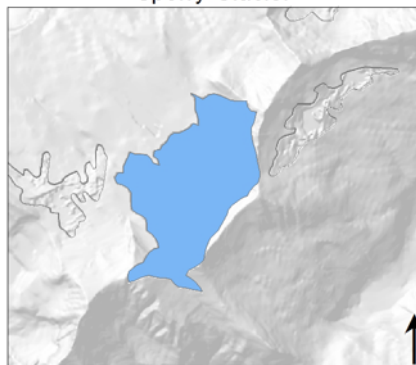
► $V^* = 3.93A^{1.124}$

- A is total area of glacier (m²)
- V is total volume of glacier (m³)

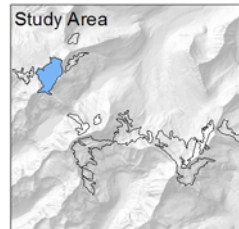


Source: Driedger and Kennard 1986

Glacier National Park, Montana Sperry Glacier



Sperry Glacier
sperrypoly
glacier13



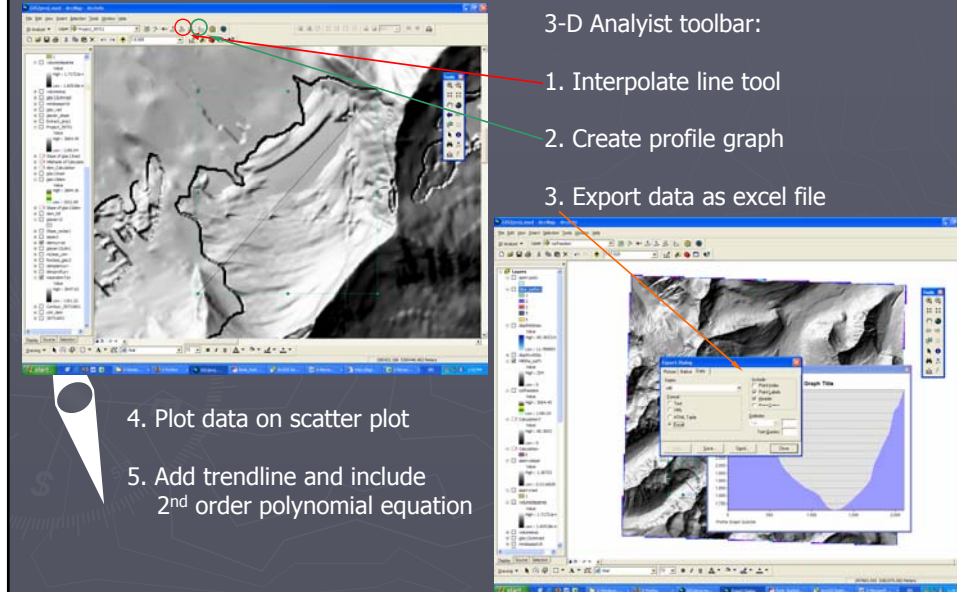
Methods: Curvature from Profiles

3-D Analyst toolbar:

1. Interpolate line tool
2. Create profile graph
3. Export data as excel file

4. Plot data on scatter plot

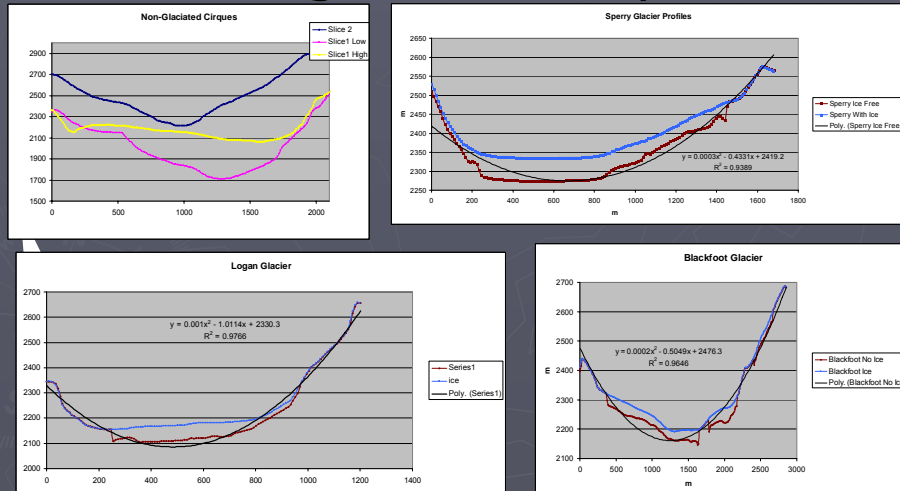
5. Add trendline and include
2nd order polynomial equation



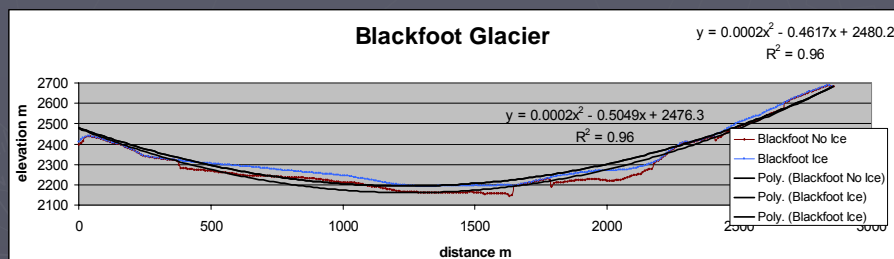
Analyzing Polynomial Equations

- ▶ The trendline of each profile generated a polynomial equation
- ▶ The second derivative of the coefficients of said polynomials are essentially the curvature value (acceleration)

Results: Profiles across glaciated and non-glaciated cirques



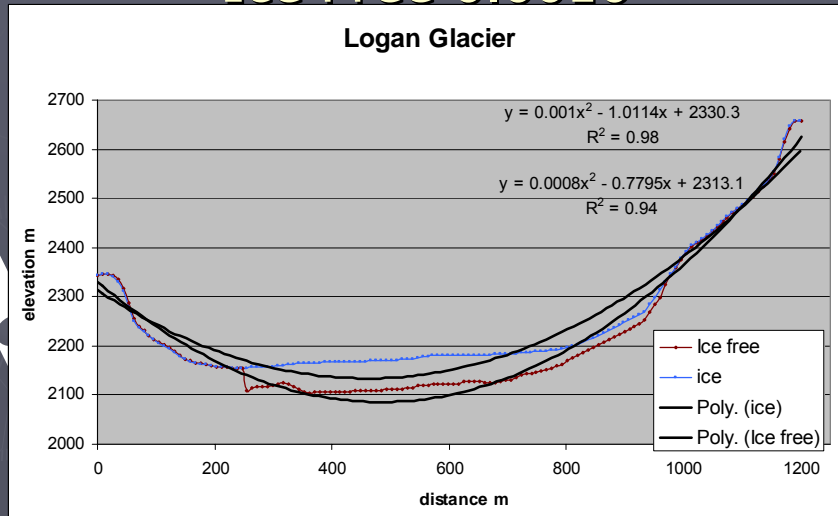
Results: Curvature Ice 0.0004 Ice Free 0.0004



Results:

Curvature Ice 0.002

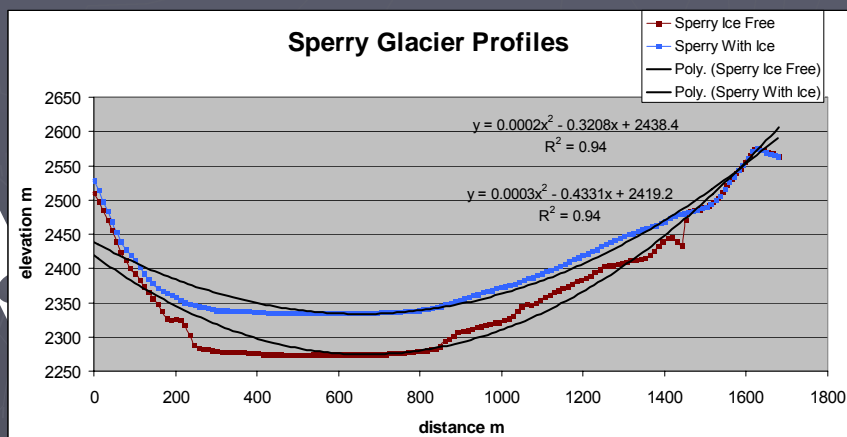
Ice Free 0.0016



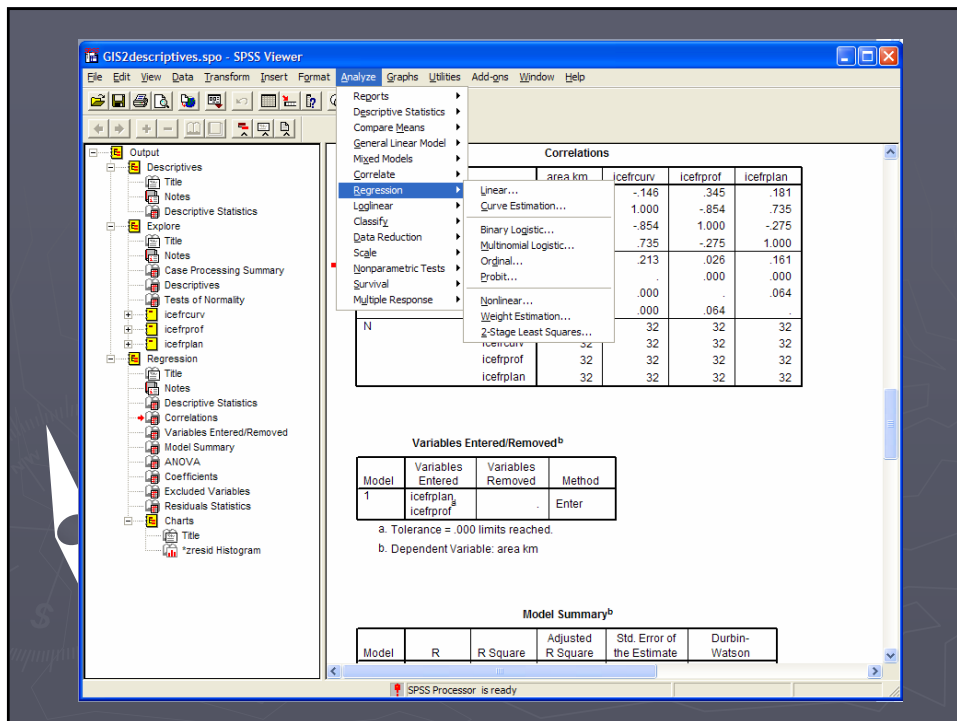
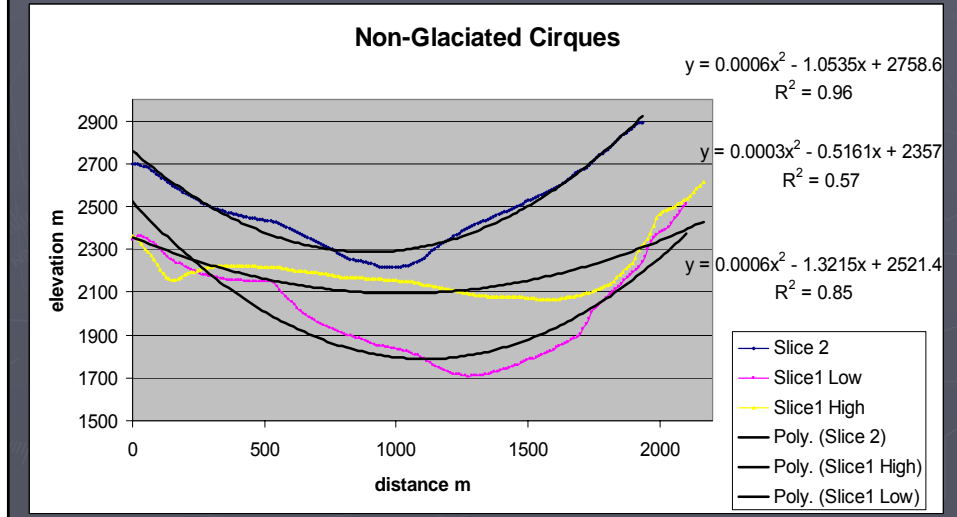
Results:

Curvature Ice 0.0004

Ice Free 0.0006



Results: Ice Free Cirque Curvature 0.0006 & 0.0003



Curvature with Ice

Correlations

		area km	precip	sol rad	plan curvature	profile	curvature	aspect	low temp mean
Pearson Correlation	area km	1.000	.048	.586	.043	.287	-.161	-.289	.091
	precip	.048	1.000	.160	.767	-.435	.620	.319	-.972
	sol rad	.586	.160	1.000	-.132	.416	-.321	.101	-.070
	plan curvature	.043	.767	-.132	1.000	-.706	.896	-.125	-.804
	profile	.287	-.435	.416	-.706	1.000	-.947	-.033	.490
	curvature	-.161	.620	-.321	.896	-.947	1.000	-.037	-.672
	aspect	-.289	.319	.101	-.125	-.033	-.037	1.000	-.229
	low temp mean	.091	-.972	-.070	-.804	.490	-.672	-.229	1.000
Sig. (1-tailed)	area km	.	.398	.000	.407	.056	.190	.055	.309
	precip	.398	.	.191	.000	.006	.000	.038	.000
	sol rad	.000	.191	.	.237	.009	.036	.291	.353
	plan curvature	.407	.000	.237	.	.000	.000	.247	.000
	profile	.056	.006	.009	.000	.	.000	.430	.002
	curvature	.190	.000	.036	.000	.000	.	.421	.000
	aspect	.055	.038	.291	.247	.430	.421	.	.104
	low temp mean	.309	.000	.353	.000	.002	.000	.104	.
N	area km	32	32	32	32	32	32	32	32
	precip	32	32	32	32	32	32	32	32
	sol rad	32	32	32	32	32	32	32	32
	plan curvature	32	32	32	32	32	32	32	32
	profile	32	32	32	32	32	32	32	32
	curvature	32	32	32	32	32	32	32	32
	aspect	32	32	32	32	32	32	32	32
	low temp mean	32	32	32	32	32	32	32	32

SPSS Regression Analysis

Correlations

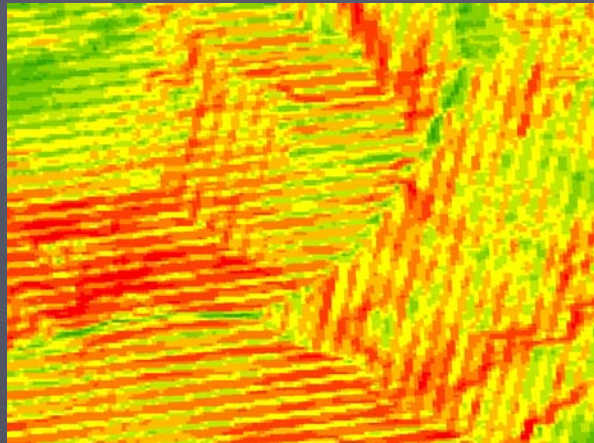
		area km	icefrcurv	icefrprof	icefrplan
Pearson Correlation	area km	1.000	-.146	.345	.181
	icefrcurv	-.146	1.000	-.854	.735
	icefrprof	.345	-.854	1.000	-.275
	icefrplan	.181	.735	-.275	1.000
Sig. (1-tailed)	area km	.	.213	.026	.161
	icefrcurv	.213	.	.000	.000
	icefrprof	.026	.000	.	.064
	icefrplan	.161	.000	.064	.
N	area km	32	32	32	32
	icefrcurv	32	32	32	32
	icefrprof	32	32	32	32
	icefrplan	32	32	32	32

Results of Analysis

- ▶ 0.345 = Pearson's correlation of curvature with area
- ▶ Based on the means at 32 elevation classes on all glaciers

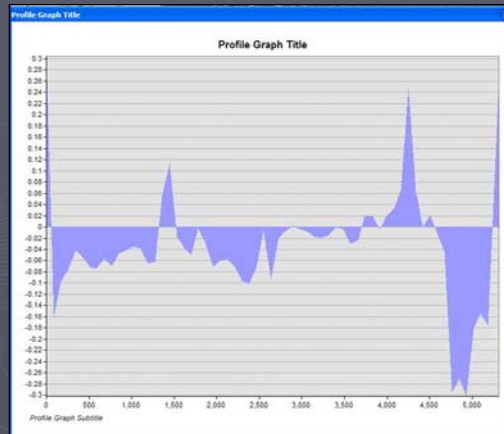
Problem #1

- ▶ Slope Calculation Tool
 - Initially generated lines that did *not at all* represent reality



Problem #2

- ▶ Curvature tool in 3-D and Spatial analyst was too refined for our scale
- ▶ Varying the cell size did not really improve results



Future Work

- ▶ Advanced GIS analysis in GRASS

$$\omega_p = -\frac{f_{xx}f_x^2 + 2f_{xy}f_xf_y + f_{yy}f_y^2}{p\sqrt{q^3}}$$

- ▶ Collect the curvature value at numerous elevations along glaciers & tabulate the data
- ▶ Update aerial photography/DEM's

Source: Bonk, 2002

Conclusions

- ▶ Remote Sensing is a useful tool for depth calculations especially with repeat aerial photography
 - Glaciological methods are limiting
 - Ground-truthing still required
- ▶ Curvature analysis requires advanced calculations or tool modifications
 - Profile slice good manual technique

Data Sources

- ▶ "Glacier National Park - Pass Trail and Feather Plume Falls." *National Park Service – Experience Your America*. 25 Aug. 2001. National Park Service. 27 May 2007
<<http://www.nps.gov/archive/glac/gallery/082501.htm>>.
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- ▶ "Montana Map." *GMT: Greenwich Mean Time - World Time / Time in every Time Zone*. 31 Jan. 2007. Greenwich 2000 Ltd. 27 May 2007
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- ▶ *National Elevation Dataset*. Aug. 2006. US Geological Survey. 17 May 2007
<<http://ned.usgs.gov/>>.
- ▶ Glacier side view <<http://www.mrsciguy.com/sciimages/alpineglacier.jpg>>

References

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- ▶ Chueca, J. and A. Julian. 2004. Relationship between solar radiation and the development and morphology of small cirque glaciers (Maladeta Mountain Massif, Central Pyrenees, Spain). *Geografiska Annaler* 86 A (1): 81-89.
- ▶ Driedger, C.L. and Kennard, P.M. "Glacier Volume Estimation on Cascade Volcanoes: An Analysis and Comparison with Other Methods." *Annals of Glaciology* 8 (1986): 59-64.
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- ▶ Graf, W.L. 1976. Cirques as glacier locations. *Arctic and Alpine Research* 8 (1): 79-90.
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