Question 3 was: How large should n be? Stat 576

Assume that our total coest is fixed

C = Co + \frac{1}{2} n_h C_h

L=1

C-Ca

C-Ca

n= C-c. Zng h=1

$$N = (C-C) \frac{\frac{1}{2} N_{1} S_{1}}{2 N_{2} S_{1} S_{2}}$$

$$\frac{1}{2} N_{2} S_{1} S_{2}$$

For Neymon allocation, $C_h = c$

This remains true for propurbional & equal allocation

Question 2 was about demarcation

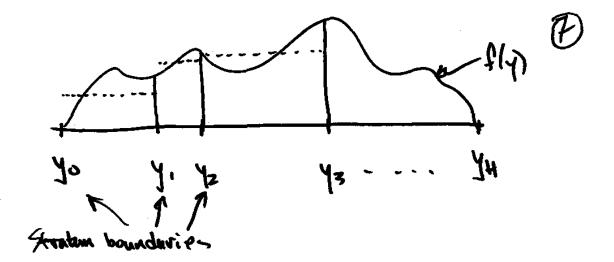
God: Mainte
$$V(y_{str}) = \sum_{h=1}^{4} \frac{N_h}{N_h} \frac{N_h}{N_h} \left(1 - \frac{N_h}{N_h}\right)$$

Approximate by ignoring the Spes

Assum that we will be using Meyonan allocation

6

Minimizing Zwy Sh will approximminize Vtyser)



Assume fly) can be approximated by a uniform density within each stratum

Now Wh = M = properties & predator in stratum h

Also, $\frac{5}{h} = papulation uniquee in statum h

<math display="block">
\frac{(y_h - y_{h-1})^2}{12} \qquad (variance of a uniform distribution)$

 $\sum_{h=1}^{2} \frac{1}{h^{2}} \sum_{h=1}^{2} \frac{1}{h^{2}} \frac{1}{h^{2}} \frac{1}{h^{2}} = \sum_{h=1}^{2} \frac{1}{h^{2}} \frac{1}{h^{2}} \frac{1}{h^{2}} \frac{1}{h^{2}} = \sum_{h=1}^{2} \frac{1}{h^{2}} \frac{1}{h^{2}} \frac{1}{h^{2}} \frac{1}{h^{2}} = \sum_{h=1}^{2} \frac{1}{h^{2}} \frac{1}{h^{2}} \frac{1}{h^{2}} \frac{1}{h^{2}} \frac{1}{h^{2}} = \sum_{h=1}^{2} \frac{1}{h^{2}} \frac{1}{h^{$

Remember, Cauchy-Schwarz says

1912 11512 = (a.b)2, with equality

When $\vec{a} = kT_0$ That is, $V(\vec{y}_{sk'})$ is (approx) minimized

When $VT_{sk}(y_{k'})$ is constant

This is the Dolenius Holges Rule

Example:

West 2

	1 1		دا ـ ا ،
Annual incom	e frey	10	mata
20 to 30°	11	3.32	
30 to 40	- 14	3.44	
40 to 50		3	
50 to 60		2	
60 to 70	5	2.24	
70 \$ 80-	8	2.83	
४० ५० भेप	. 3	1.13	
90 40 100	- 2	1.41	
	•	20.27	

First guess: Use the Cumulative square rook frequency (CSRF) Tale - divide the total square-root frq. by the desired # It strata

20.27 = 10.135

Check your results: The (yh-yh)
7
134 (50-20) \$\frac{7}{2} \lefta \frac{1}{2} \left(\text{for 50} \)
175 235

(13)

Trital ? error: more each boundary up 1 Space + down 1 space + see & you get an importance 138 (60-20) 2 TB (140-60) 246 109

Suppose that we can come close to Dalenais Hudges and that we are using Ulyman allocation

$$\int_{A} = \frac{N_h S_h}{\sum_{h=1}^{N} N_h S_h} \cdot n = \frac{N_h S_h}{\sum_{h=1}^{N} N_h S_h} \cdot n$$

$$= \frac{N_h S_h}{\sum_{h=1}^{N}$$

一点红外一小了一点强

Dalenius. Hutges solution was to make an constat

.. $n_k = \frac{n}{H}$, which is excel allocation

Summary: To minimize Vityser, use D-H rule to And the boundaries + then apply great allocation!!

In Exercise 6 of Chapter 2, data on numbers of publications were given for an SRS of 50 faculty members. Not all departments were represented, however, in the SRS. The SRS contained several faculty members from psychology and from chemistry, but none from foreign languages. The following data are from a stratified sample of faculty, using the areas biological sciences, physical sciences, social sciences, and humanities as the strata.

Stratum	Number of Faculty Members in Stratum	Number of Faculty Members in Sample	
Biological Sciences	102		
Physical Sciences	310	19	
Social Sciences	217	13	
Humanities	178	11	
Total	807	50	

The frequency table for number of publications in the strata is given below.

Number of	Number of Faculty Members			
Refereed Publications	Biological	Physical	Social	Humanities
0	1	10	9	8
1	2	2	0	2
2	0	0	1	0
3	1	1	0	1
4	0	2	2	0
5	2	1	0	0
6	0	1	1	0
7	1	O	0	0
8	0	2	0	0

- **a** Estimate the total number of refereed publications by faculty members in the college, and give the standard error.
- b How does your result from (a) compare with the result from the SRS in Exercise 6 of Chapter 2?
- **c** Estimate the proportion of faculty with no refereed publications, and give the standard error.
- **d** Did stratification increase precision in this example? Explain why you think it did or did not.

- A public opinion researcher has a budget of \$20,000 for taking a survey. She knows that 90% of all households have telephones. Telephone interviews cost \$10 per household; in-person interviews cost \$30 each if all interviews are conducted in person, and \$40 each if only nonphone households are interviewed in person (because there will be extra travel costs). Assume that the variances in the phone and nonphone groups are similar, and that the fixed costs are $c_0 = 5000 . How many households should be interviewed in each group if
 - a all households are interviewed in person
 - **b** households with a phone are contacted by telephone and households without a phone are contacted in person.