

Q733-1

Resources on Mathematical Ideas Among the Indigenous Peoples of Latin America

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NUMERATION AND CALCULATION

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