

## Period of a Pendulum.

$$F = mg \sin \theta$$

When assuming  $\theta$  is small,  $\sin \theta$  is  $\theta$  itself,  $\sin \theta \approx \theta$

$$\theta = \frac{s}{L}, \quad s \text{ is arc length.}$$

$$F = mg \sin \theta \approx mg \theta = \left( \frac{mg}{L} \right) s.$$

In the case of a mass on a spring,  $F = kx$ . If we let  $x = s$

$$F = ks = k \cdot \frac{F \cdot L}{mg}$$

$$k = \frac{mg}{L}$$

Therefore, period,  $T = 2\pi \sqrt{\frac{m}{k}} = 2\pi \sqrt{\frac{m}{mg/L}}$

$$\boxed{T = 2\pi \sqrt{\frac{L}{g}}}$$

\*  $T$  is independent of mass and amplitude.

- A larger mass tends to move more slowly because of its inertia
- The larger mass the greater  $g$  force acting on it.

## Period of a Physical Pendulum

$$T = 2\pi \sqrt{\frac{I}{mgL}}$$

The moment of Inertia,  $I = mL^2$ .

