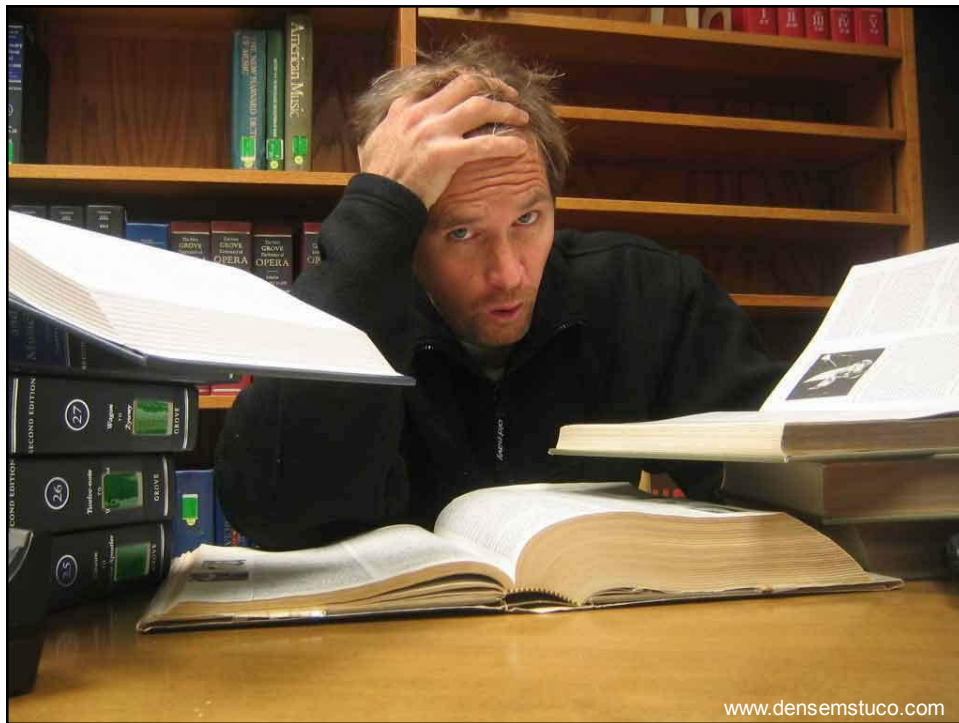
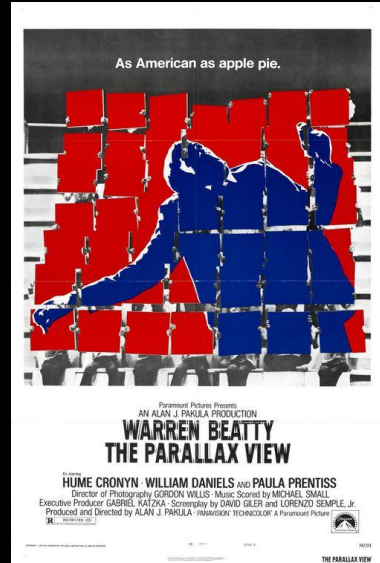
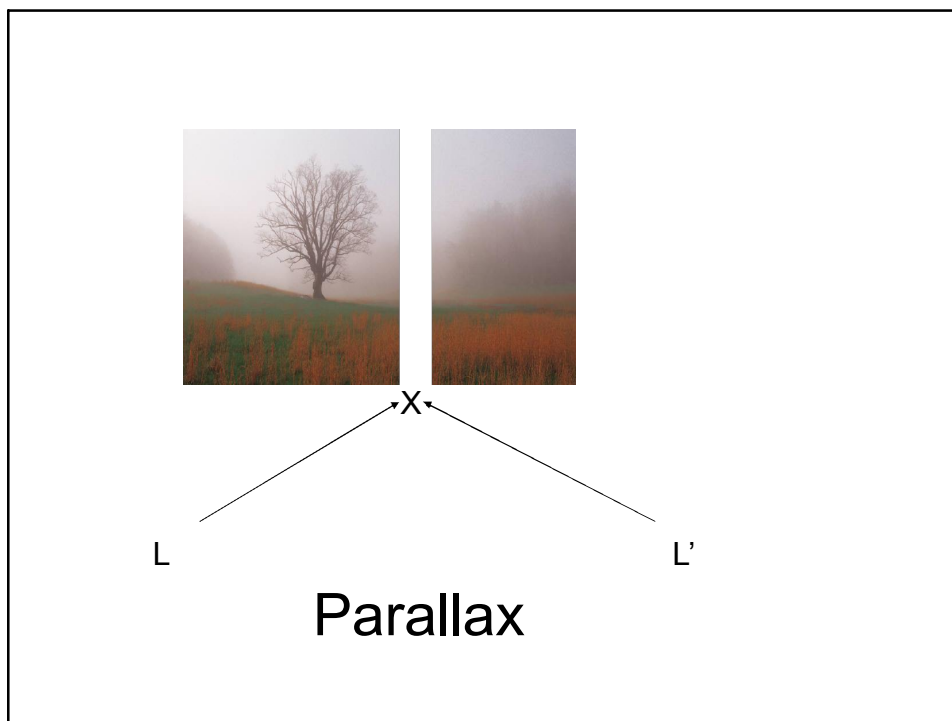


# Image Parallax

Disclaimer:

The extent of my knowledge of parallax prior to this week.



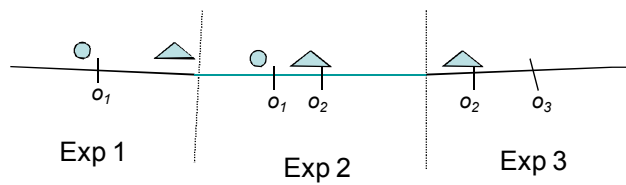


## Image Parallax (Lillesand *et al*, 2004)

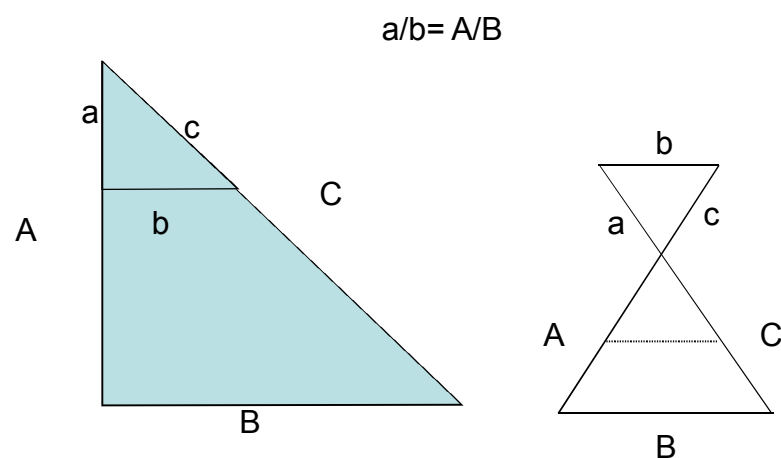
“The apparent change in relative positions of stationary objects caused by a change in viewing position.”

Thus, pairs of images. For photogrammetry, we use overlapped images, forming a stereopair.

“Parallax displacements occur only parallel to the line of flight.”  
 (Lillesand *et al*, 2004)



Parallax equations rely on similar triangles



## Similar Triangles

Assumptions: truly vertical photographs  
and constant flight height.

Without these conditions, the triangles  
drawn would not be similar.

## Terms/Symbols

$p_a$  = parallax of point  $a$  measured in image

$f$  = focal length of lens

$H$  = flight height relative to datum

$B$  = air base, i.e. distance between exposures

$L$  = exposure station    $L'$  = subsequent exposure station

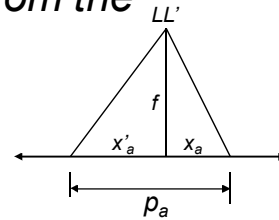
$x_a$  = x-coordinate within left/first image

$X_A$  = X-coordinate of feature at ground

$x'_a$  = x-coordinate of feature within right/second image

## Similar Triangles

Create a compound triangle from the exposures/photos



Then:

$\rho_a$  corresponds to **B** (distance between 2 exposures)

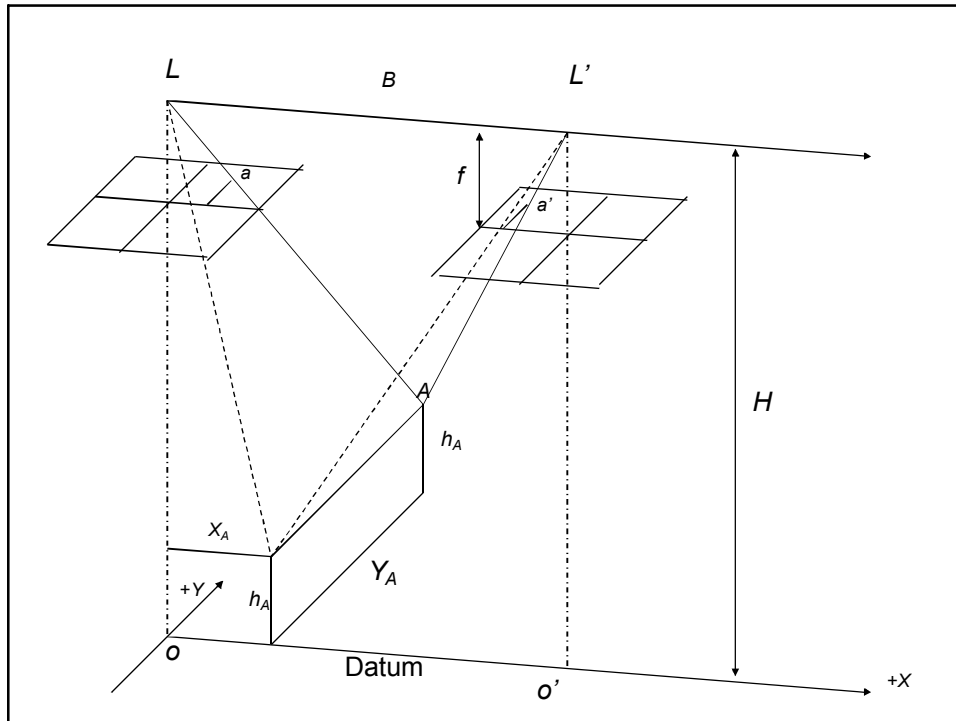
$f$  corresponds to  $H - h_A$  (total height minus elevation of point A)

### Leading us to...

$$\frac{\rho_a}{f} = \frac{B}{H - h_A}$$

$$h_A = H - \frac{Bf}{\rho_a}$$

$h_A$  is the z-value of A



## More parallax equations

$$\frac{X_A}{H-h_A} = \frac{X_a}{f}$$

$$X_A = \frac{x_a(H-h_A)}{f}$$

remember

$$H-h_A = Bf/p_a$$

$$X_A = B(X_a/p_a)$$

## Problem

Lens ( $f$ )= 150 mm

Flying height ( $H$ )= 1000m

Air base ( $B$ )= 800m

$x_a$ = 55mm

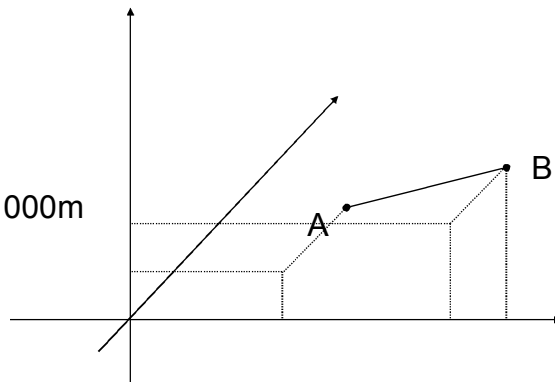
$x_b$ = 140mm

$y_a$ = 100mm

$y_b$ = 150mm

$x'_a$ = -95mm

$x'_b$ = -20mm



Find the X, Y, Z  
coordinates of Points  
A and B.

## Alternative methods

- Aligning flight lines ( $p = D-d$ )
- Stereoscopic viewing (floating mark/parallax wedge)
- Computer: image correlation