

## Hypothesis test for $p$

$$\begin{array}{l|l|l} H_0: p = p_0 & H_0: p \leq p_0 & H_0: p \geq p_0 \\ H_1: p \neq p_0 & H_1: p > p_0 & H_1: p < p_0 \end{array}$$

Use the  $z$ -table

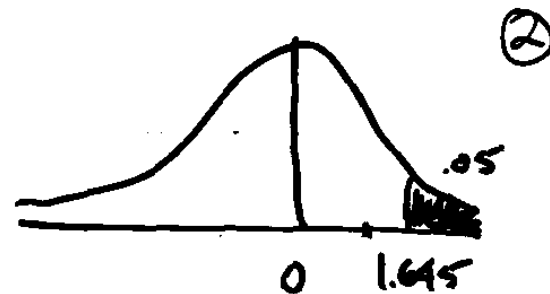
$$\text{Test stat} = z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$$

Example: In a sample of 100 voters, 55 favor a ballot measure.

At the 5% level of significance, can we conclude that more than 50% of all voters favor the measure?

①  
452  
4-27

$$\begin{array}{l} H_0: p \leq .5 \\ H_1: p > .5 \end{array}$$



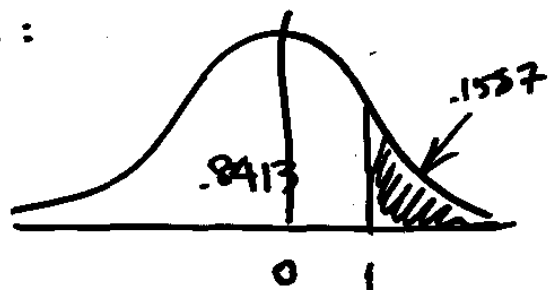
$$n = 100$$

$$\hat{p} = \frac{55}{100} = .55$$

$$z = \frac{.55 - .5}{\sqrt{\frac{(.5)(.5)}{100}}} = 1$$

Accept  $H_0$ . We were unable to show that more than 50% of voters favor the measure.

p-value:



p-value = .1587

③

$$t = \frac{\bar{X}_1 - \bar{X}_2 - d_0}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}}$$

df = same as for C.I.s

④

Comparing 2 population means

$$\begin{array}{l} H_0: \mu_1 - \mu_2 = d_0 \\ H_1: \mu_1 - \mu_2 \neq d_0 \end{array} \quad \text{etc.}$$

$$\text{Test stat} = z = \frac{\bar{X}_1 - \bar{X}_2 - d_0}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$$

OR

Comparing 2 proportions

$$\begin{array}{l} H_0: p_1 - p_2 = d_0 \\ H_1: p_1 - p_2 \neq d_0 \end{array} \quad \text{etc.}$$

(The  $d_0$  is almost always 0)

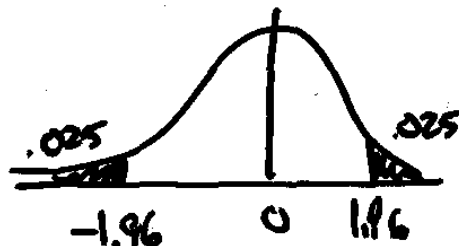
$$\text{Test stat} = z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\hat{p}\hat{q}\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}}$$

$$\text{where } \hat{p} = \frac{n_1 \hat{p}_1 + n_2 \hat{p}_2}{n_1 + n_2} \quad (5)$$

Example: See if the defect rates for 2 manufacturing processes are different. Use  $\alpha = .05$

$$H_0: p_1 - p_2 = 0$$

$$H_a: p_1 - p_2 \neq 0$$



Collect the data:

$$n_1 = 80$$

$$x_1 = 5$$

$$\hat{p}_1 = \frac{5}{80} = .0625$$

$$n_2 = 60$$

$$x_2 = 6$$

$$\hat{p}_2 = \frac{6}{60} = .1$$

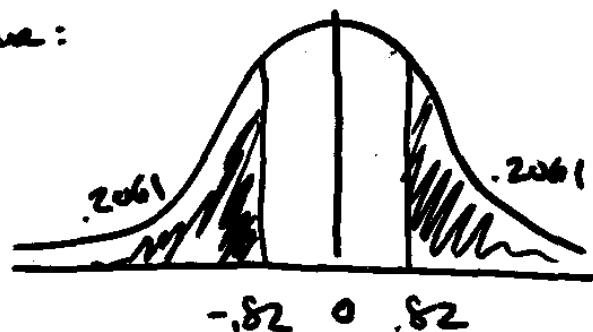
$$\hat{p} = \frac{80(\frac{5}{80}) + 60(\frac{6}{60})}{80 + 60} \quad (6)$$

$$= \frac{5 + 6}{80 + 60} = \frac{11}{140} = .0786$$

$$Z = \frac{.0625 - .1}{\sqrt{(.0786)(.9214)(\frac{1}{80} + \frac{1}{60})}} = -1.82$$

Accept  $H_0$ . We failed to detect a difference between the 2 defect rates.

p-value:



p-value = .4122

Matched pairs

$$\begin{array}{l|l} H_0: \mu_d = d_0 & \\ H_1: \mu_d \neq d_0 & \text{etc} \end{array}$$

$$\text{Test stat} = t = \frac{\bar{d} - d_0}{s_d / \sqrt{n}}$$

⑦

Example: 200 matched pairs of Supermarkets.

In the "A" half of each pair, a new product is introduced, but not in the "B" half.

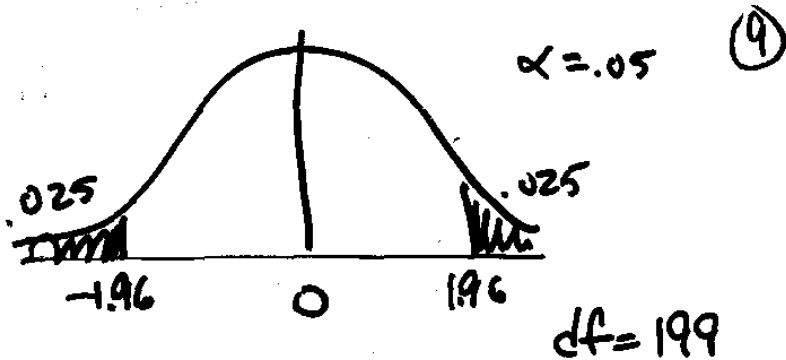
A	B
173	168
211	214
200	190
⋮	⋮

} 200 data points.

Test for a change in either direction.

$$\begin{array}{l} H_0: \mu_d = 0 \\ H_1: \mu_d \neq 0 \end{array}$$

⑧



Say  $\bar{d} = -20$  and  $s_d = 2$

$$t = \frac{-20 - 0}{2/\sqrt{200}} = -141$$

Reject  $H_0$ . Sales were significantly lower at the "A" stores.

p-value  $\approx 0$

HW #5 p. 357 10.24

10.46

10.51

p. 366 10.56

10.66

due Tuesday, May 4

Midterm is also May 4

(10)